

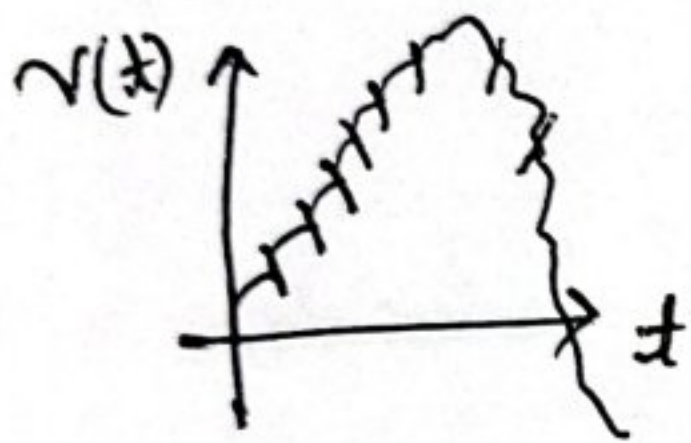
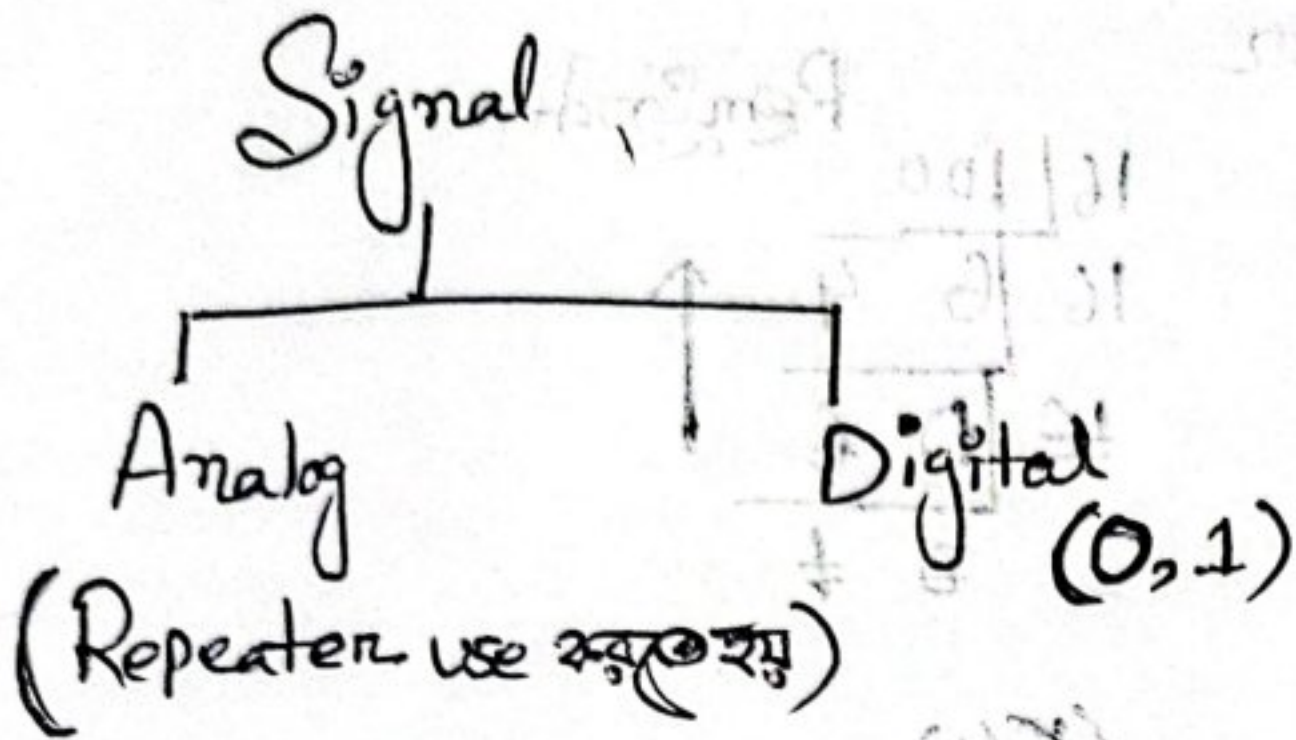
# Digital Logic design

21-01-2024

Sunday



Logic  $\rightarrow$  Condition



- ① Number System
- ② Boolean Algebra
- ③ Combinational Logic Circuit
- ④ Sequential Logic Circuit

Number  $\rightarrow$  मापना किन्तु Measure/quantify करवा उन्हा use करा शक्य।

## ① Number System

**Base** is the number of unit digits used in a number System.

	Base (digit)
Decimal	$\rightarrow 0-9$
Binary	$\rightarrow 0, 1$
Octal	$\rightarrow 0-7$
Hexadecimal	$\rightarrow 0-9, A, B, C, D, E, F$

# Decimal to other number System

$$(100)_{10} = (?)_2 = (?)_8 = (?)_{16}$$



उदाहरण

	Remainder
2   100	
2   50	0
2   25	0
2   12	1
2   6	0
2   3	0
2   1	1
	0 1

	Remainder
8   100	
8   12	4
8   4	4
	0 1

	Remainder
16   100	
16   6	4
	0 6

$$= (144)_8$$

$$= (64)_{16}$$

$$= (1100100)_2$$

$$(100)_{10} = (1100100)_2 = (144)_8 = (64)_{16}$$

$$(126.56)_{10} = (?)_8$$

	Remainder
8   126	
8   15	6
8   1	7
	0 1

$$(126)_{10} = (176)_8$$

$$\therefore (126.56)_{10} = (176.4365)_8$$

0.56	
x 8	
4	.48
x 8	
3	.84
x 8	
6	.72
x 8	
5	.76

$$(0.56)_{10} = (0.4365)_8$$

From other number system to decimal

\*  $(1101)_2 = (?)_{10}$

$= 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$

$= 8 + 4 + 2 + 1$

$= (15)_{10}$

$\therefore (1101)_2 = (15)_{10}$

\*  $(347)_8 = (?)_{10}$

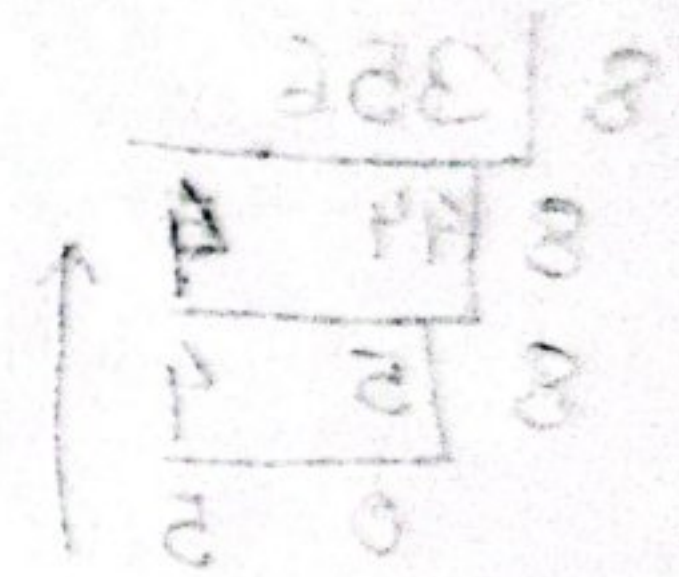
$= 3 \times 8^2 + 4 \times 8^1 + 7 \times 8^0$

$= 192 + 32 + 7$

$= (231)_{10}$

$\therefore (347)_8 = (231)_{10}$

8x	8x	8x	8x	8x
8x	8x	8x	8x	8x
8x	8x	8x	8x	8x
8x	8x	8x	8x	8x
8x	8x	8x	8x	8x



$(347)_8 = (231)_{10}$

421  
010  
 $ABC + \overline{A}BC + A\overline{B}C$

\*  $(7A3.1B)_{16} = (?)_{10}$

$= 7 \times 16^2 + A \times 16^1 + 3 \times 16^0 + 1 \times 16^{-1} + 11 \times 16^{-2}$

$= 1792 + 160 + 3 + 0.0625 + 0.04296875$

$= (1955.1054)_{10}$

\*  $(356.82)_{10} = (?)_8$

Remainder

8	356
8	44
8	54
	05

Whole Number	.82
	$\times 8$
6	.56
	$\times 8$
4	.48
	$\times 8$
3	.84
	$\times 8$
6	.72

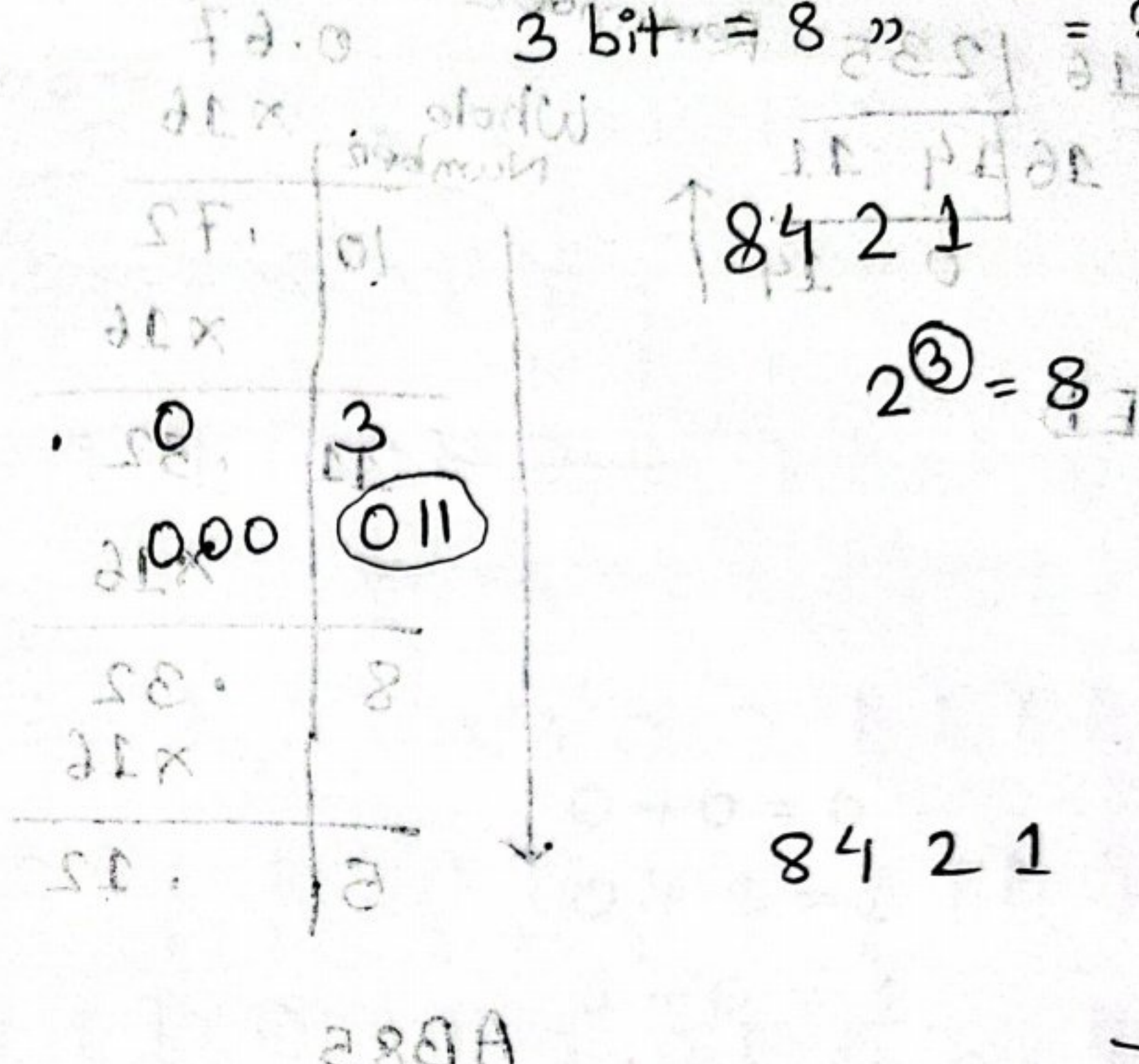
$(356.82)_{10} = (544.6436)_8$

# Octal to Binary

1 bit = 2 combinations =  $2^{1-1}$   
 2 bit = 4 " =  $2^2$   
 3 bit = 8 " =  $2^3$

$(247.03)_8 = (?)_2$

2	4	7	0	3
010	100	111	000	011



\*  $(156.46)_8 = (?)_2$

1	5	6	4	6
001	101	110	100	110

$(156.46)_8 = (00110110.100110)_2$

\*  $(ABC.DEF)_{16} = (?)_2$

A	B	C	D	E	F
1010	1011	1100	1101	1110	1111

$(ABC.DEF)_{16} = (101010111100.110111101111)_2$

\*  $(235.67)_8 = (?)_{16}$

16	235	Remainder	0.67
16	14	11	× 16
	0	14	10
			.72
			× 16
			11
			.52
			× 16
			8
			.32
			× 16
			5
			.12

Whole Number

AB85

EB

$(EB.AB85)_{16}$

\*  $(235.67)_8 = (?)_{16}$

2      3      5      6      7

010    011    101    110    111

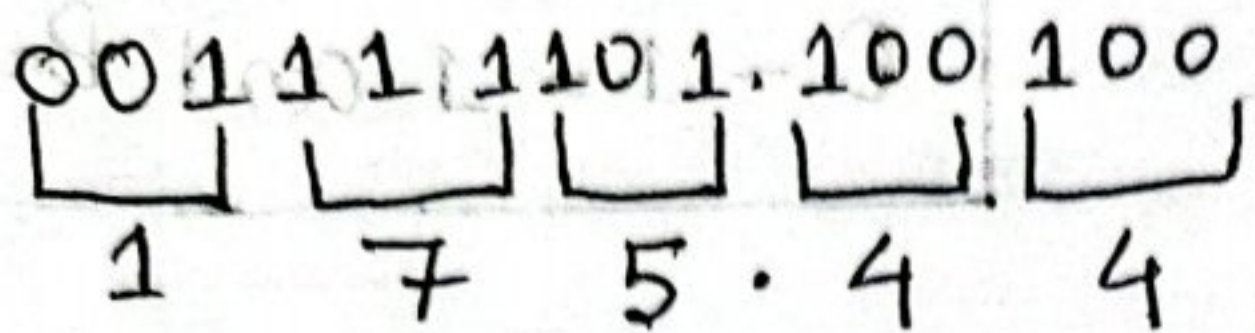
010011101.11011100

$(01001101.D01C)_{16}$

8421

\*  $(1111101.10010)_2 = (?)_8$

4 2 1



$(175.44)_8$

# Binary Addition

\* 
$$\begin{array}{r} 111111111 \\ 1101100.110 \\ 00100110 \\ + 0110111.011 \\ \hline \end{array}$$

$10100100.001$

$0+0=0$   
 $0+1=1$   
 $1+0=1$   
 $1+1=0$  Carry 1

\*  $1111$

# \* Binary Subtraction

$$0 - 0 = 0$$

$$1 - 0 = 1$$

$$1 - 1 = 0$$

$$0 - 1 = 1 \text{ and Borrow}$$

$$1101100.110$$

$$\begin{array}{r} 1101100.110 \\ - 0110111.011 \\ \hline 0110101.011 \end{array}$$

$$11110000.01011$$

$$\begin{array}{r} 11110000.01011 \\ - 01100101.11100 \\ \hline 10001001.01111 \end{array}$$

Binary Addition

1	1	1	1	1	1	1	1	1	1
0	1	1	0	1	1	0	1	1	0
0	1	0	0	0	0	0	0	0	0
1	1	0	1	1	0	1	1	0	1

$$100.0010000$$

$$1111$$

①  $(379.56)_{10} = (?)_8 = (?)_{16}$

Remainder

8	379
8	473
8	57
	05

Whole Number	0.56
	$\times 8$
4	.48
	$\times 8$
3	.84
	$\times 8$
6	.72
	$\times 8$
5	.76

$(379.56)_{10} = (573.4365)_8$

Remainder

16	379
16	2311
16	17
	01

Whole Number	.56
	$\times 16$
8	.96
	$\times 16$
F	.36
	$\times 16$
5	.76
	$\times 16$
12	.16

17B.

$(379.56)_{10} = (17B.8F5C)_{16}$

$\therefore (379.56)_{10} = (573.4365)_8 = (17B.8F5C)_{16}$



# 2's complement

28-01-2024



$$(10)_{10} \rightarrow (00001010)_2$$

$$(8)_{10} \rightarrow (00001000)_2$$

$$\begin{array}{r} \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \\ 11110111 \end{array} \text{ (1's complement)}$$

$$\begin{array}{r} + 1 \\ \hline (-8)_{10} \rightarrow 11111000 \text{ (2's complement)} \end{array}$$

$$(10)_{10} \rightarrow \overset{1}{0} \overset{1}{0} \overset{1}{0} \overset{1}{0} 1010 \quad A = 1 \cdot A$$

$$(8)_{10} \rightarrow 11111000$$

$$(2)_{10} \rightarrow 1(00000010)$$

Identity law:  $A + 0 = A$

Domination

8 4 2 1

$$1 = 1 + 0$$

$$1 = 1 + 1$$



$$(125)_{10} - (59)_{10}$$

$$A \cdot B = B \cdot A$$

$$A + B = B + A$$

$$(125)_{10} \rightarrow (01111101)_2$$

$$(59)_{10} \rightarrow (00111011)_2$$

$$\begin{array}{r} \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \\ 11000100 \end{array}$$

1's complement

$$+ 1$$

$$\begin{array}{r} (-59)_{10} = 11000101 \end{array}$$

$$(125)_{10} \rightarrow 01111101$$

$$(-59)_{10} \rightarrow 11000101$$

$$(66)_{10} \rightarrow 1(01000010)$$

2's complement

$$(A+B) \cdot (A+B) = (A+B) + (A+B)$$

$$A + AC + AB + BC = A + AC + AB + BC$$

$$= A + (A + C + B) + BC$$

$$= A + 1 + BC$$

# Boolean Algebra

Boolean variable is a variable that has only two values: either 0 or 1.

## Postulates and Theorems:

① Identity law:  $A + 0 = A$

$$A \cdot 1 = A$$

② Dominance law:

$$A + 1 = 1$$

$$A \cdot 0 = 0$$

$$0 + 1 = 1$$

$$0 \cdot 0 = 0$$

$$1 + 1 = 1$$

$$1 \cdot 0 = 0$$

Level निम्न क्रम में,

③ Commutative law:  $A + B = B + A$

$$A \cdot B = B \cdot A$$

④ Distributive law:  $A \cdot (B + C) = A \cdot B + A \cdot C$

⑤ Complimentary law:

$$A + \bar{A} = 1$$

$$A \cdot \bar{A} = 0$$

$$0 + 1 = 1$$

$$0 \cdot 1 = 0$$

$$1 + 0 = 1$$

$$1 \cdot 0 = 0$$

⑥ Double negation law:  $\bar{\bar{A}} = A$

$$A = 0, \bar{A} = 1, \bar{\bar{A}} = 0$$

⑦  $A + BC = (A + B) \cdot (A + C)$

\*  $A \cdot A = A$

$$= A \cdot A + A \cdot C + B \cdot A + B \cdot C$$

$A + A = A$

$$= A + AC + AB + BC$$

$$= A + (1 + C + B) + BC$$

$$= A \cdot 1 + BC$$

$$= A + BC$$

⑧ De-Morgan's theorem:

(i)  $\overline{A+B} = \overline{A} \cdot \overline{B}$

(ii)  $\overline{A \cdot B} = \overline{A} + \overline{B}$

30-01-2024

\*  $(123)_{10} - (85)_{10}$  using 2's complement

64 32 16 8 4 2 1

$(123)_{10} \rightarrow 01111011$

$(85)_{10} \rightarrow 01010101$   
 $\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$   
 $10101010$

1's complement

$(85)_{10} = 10101011$

2's complement +

$(123)_{10} \rightarrow 01111011$

$(-85)_{10} \rightarrow 10101011$

$(38)_{10} \rightarrow 100100110_2$

$\overline{\overline{A}} = A$   
 $\overline{A \cdot B} = \overline{A} + \overline{B}$  ①

$\overline{\overline{A} + \overline{B}} = A \cdot B$  ②

A	B	$\bar{A}$	$\bar{B}$	A+B	$\overline{A+B}$	$\bar{A} \cdot \bar{B}$	A · B	$\overline{A \cdot B}$	$\overline{A+B}$
0	0	1	1	0	1	1	0	1	1
0	1	1	0	1	0	0	0	1	1
1	0	0	1	1	0	0	0	1	1
1	1	0	0	1	0	0	1	0	0

Proof of De Morgan's

1.  $\overline{A+B+C} = \bar{A} \cdot \bar{B} \cdot \bar{C}$

2.  $\overline{A \cdot B \cdot C} = \bar{A} + \bar{B} + \bar{C}$

Theorem (22) - (23) \*

A	B	C	$\bar{A}$	$\bar{B}$	$\bar{C}$	A+B+C	$\overline{A+B+C}$	$\bar{A} \cdot \bar{B} \cdot \bar{C}$	A · B · C	$\overline{A \cdot B \cdot C}$	$\bar{A} + \bar{B} + \bar{C}$
0	0	0	1	1	1	0	1	1	0	1	1
0	0	1	1	1	0	1	0	0	0	1	1
0	1	0	1	0	1	1	0	0	0	1	1
0	1	1	1	0	0	1	0	0	0	1	1
1	0	0	0	1	1	1	0	0	0	1	1
1	0	1	0	1	0	1	0	0	0	1	1
1	1	0	0	0	1	1	0	0	0	1	1
1	1	1	0	0	0	1	0	0	1	0	0

①  $\overline{A_1 + A_2 + A_3 + \dots + A_n} = \bar{A}_1 \cdot \bar{A}_2 \cdot \bar{A}_3 \dots \bar{A}_n$

②  $\overline{A_1 \cdot A_2 \cdot A_3 \dots A_n} = \bar{A}_1 + \bar{A}_2 + \bar{A}_3 + \dots + \bar{A}_n$

# Logic Gate

AND (·)

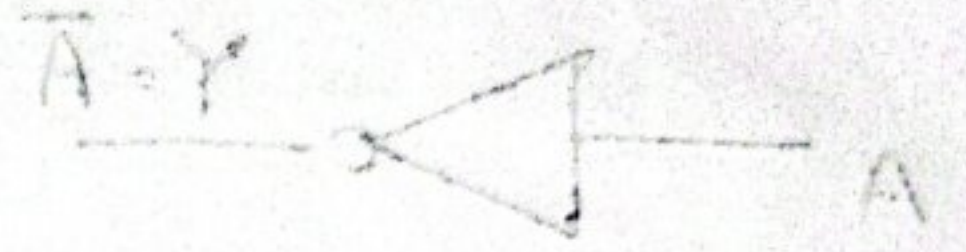
OR (+)

NOT (-)

Order of preference

Parenthesis NOT AND OR

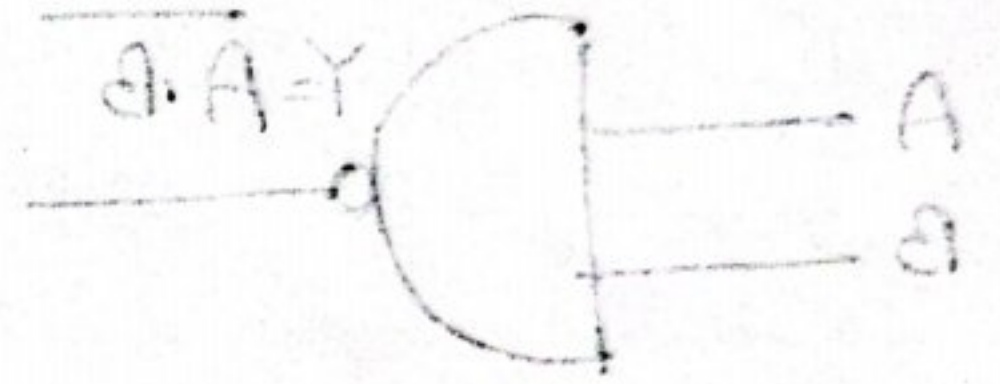
NOT: Expression  $\bar{A} = Y$



Logic Gate is an electronic circuit that can perform boolean operations.

AND:

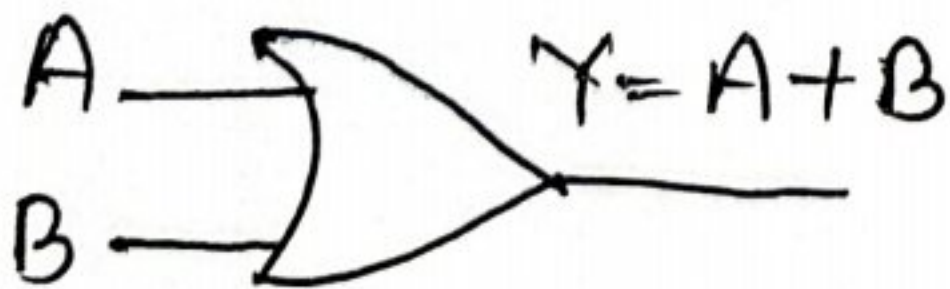
Expression  $Y = A \cdot B$



A	B	A · B
0	0	0
0	1	0
1	0	0
1	1	1

OR:

Expression  $Y = A + B$

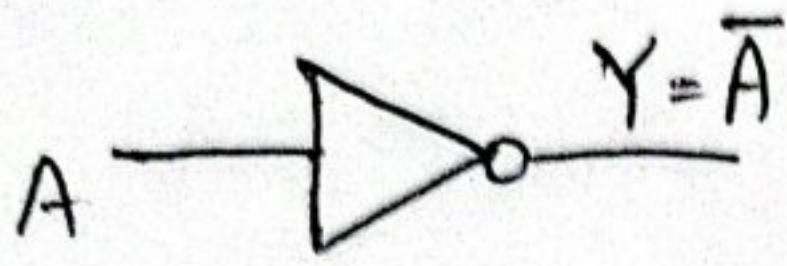


A	B	A + B
0	0	0
0	1	1
1	0	1
1	1	1

A	B	A + B
0	0	0 + 0 = 0
0	1	0 + 1 = 1
1	0	1 + 0 = 1
1	1	1 + 1 = 1



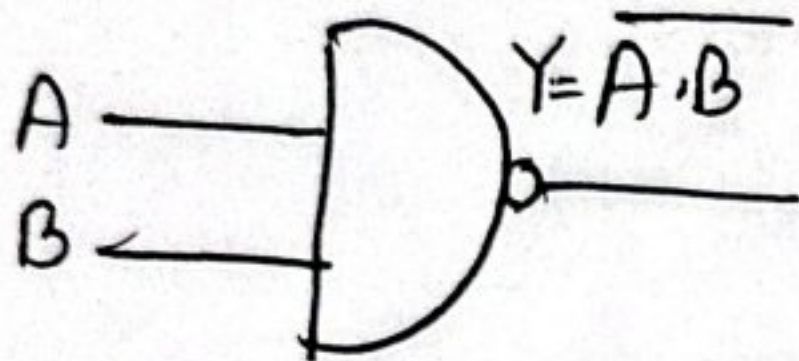
NOT: Expression  $Y = \bar{A}$



A	$\bar{A}$
0	1
1	0

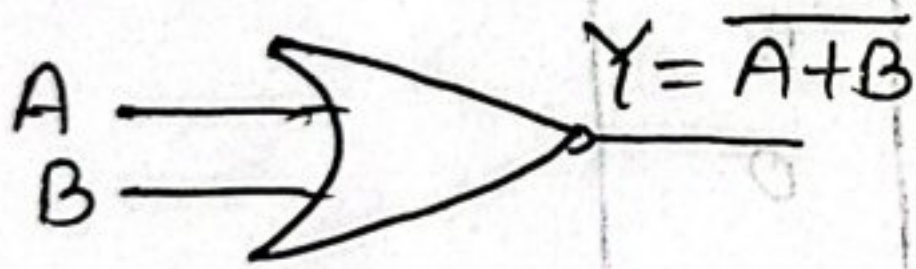
(.) AND  
(+) OR  
(-) NOT

NAND: Expression  $Y = \overline{A \cdot B}$



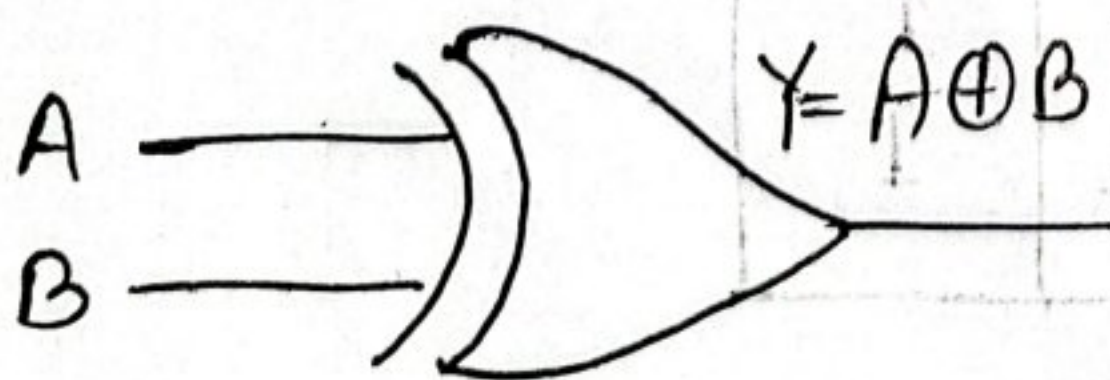
A	B	$\overline{A \cdot B}$
0	0	1
0	1	1
1	0	1
1	1	0

NOR: Expression  $Y = \overline{A + B}$



A	B	$\overline{A + B}$
0	0	1
0	1	0
1	0	0
1	1	0

X-OR: Expression  $Y = A \oplus B = \bar{A}B + A\bar{B}$



A	B	$\bar{A}B + A\bar{B}$
0	0	$1 \cdot 0 + 0 \cdot 1 = 0$
0	1	$1 \cdot 1 + 0 \cdot 0 = 1$
1	0	$0 \cdot 0 + 1 \cdot 1 = 1$
1	1	$0 \cdot 1 + 1 \cdot 0 = 0$

XNOR: Expression

$$Y = \overline{A \oplus B}$$

De Morgan's theorem

$$= \overline{AB + A\bar{B}} = \overline{AB} \cdot \overline{A\bar{B}} \quad \text{1st}$$



$$= (\overline{A+B}) \cdot (\overline{A+\bar{B}}) \quad \text{2nd}$$

$$= (A+\bar{B}) \cdot (\bar{A}+B)$$

$$= A \cdot \bar{A} + A \cdot B + \bar{B} \cdot \bar{A} + \bar{B} \cdot B$$

$$= 0 + A \cdot B + \bar{A} \cdot \bar{B} + 0$$

$$= AB + \bar{A} \cdot \bar{B}$$

A	B	$Y = AB + \bar{A} \cdot \bar{B}$
0	0	$0 + 1 = 1$
0	1	$0 \cdot 1 + 1 \cdot 0 = 0$
1	0	$1 \cdot 0 + 0 \cdot 1 = 0$
1	1	$1 \cdot 1 + 0 \cdot 0 = 1$

04-02-2024

Boolean Function

$$F(x, y) = (x+y) \cdot (x+y')$$

$$= x \cdot x + x \cdot y' + y \cdot x + y \cdot y'$$

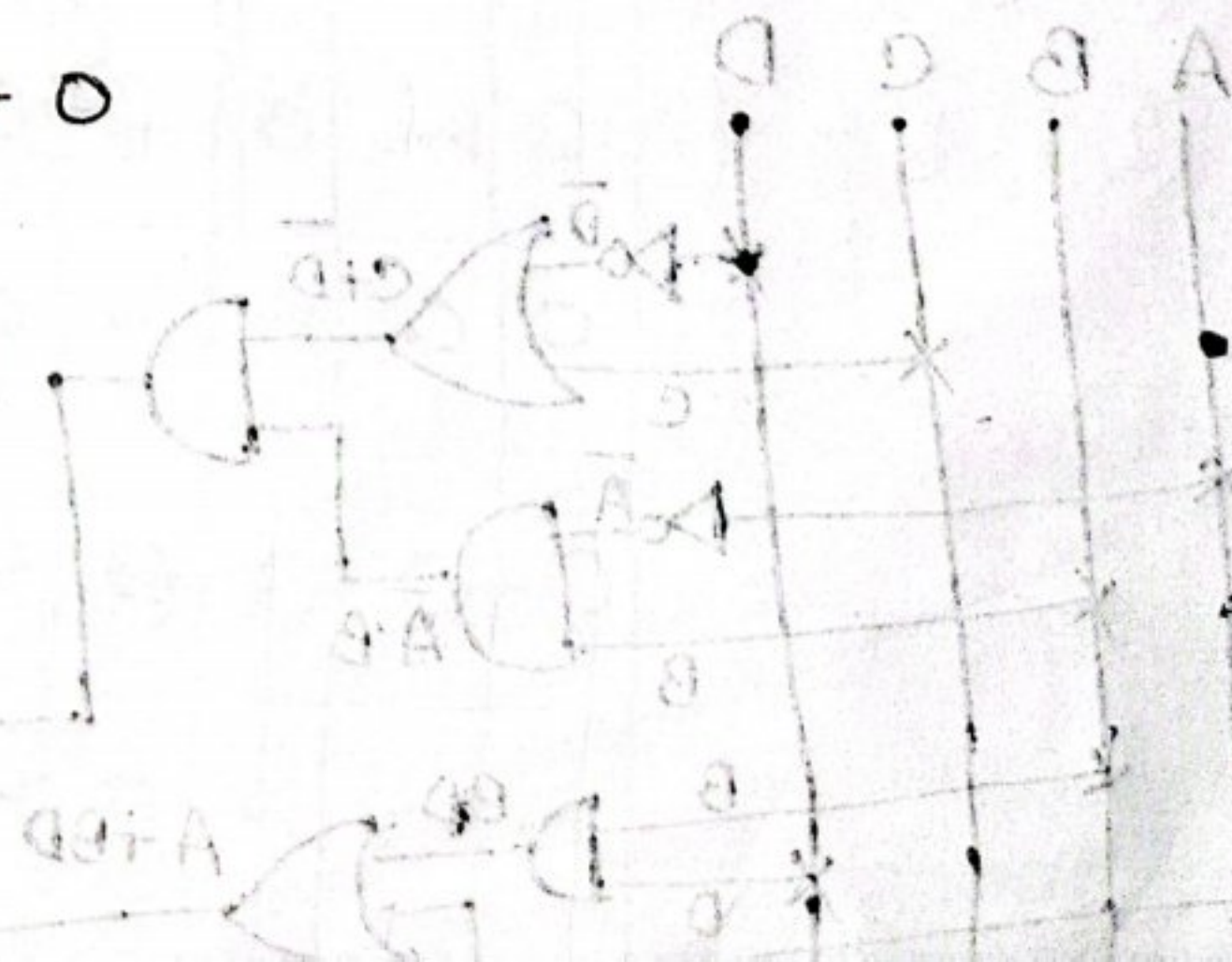
$$= x + x \cdot y' + y \cdot x + 0$$

$$= x(1 + y' + y)$$

$$= x \cdot 1 = x$$

\* Importance of

Simplification of  
Boolean function



\*  $(x+y)(x+z)(y+z)$

$= (x+y)(x'y + x'z + yz + z \cdot z)$

$= (x+y)(x'y + x'z + yz + z)$

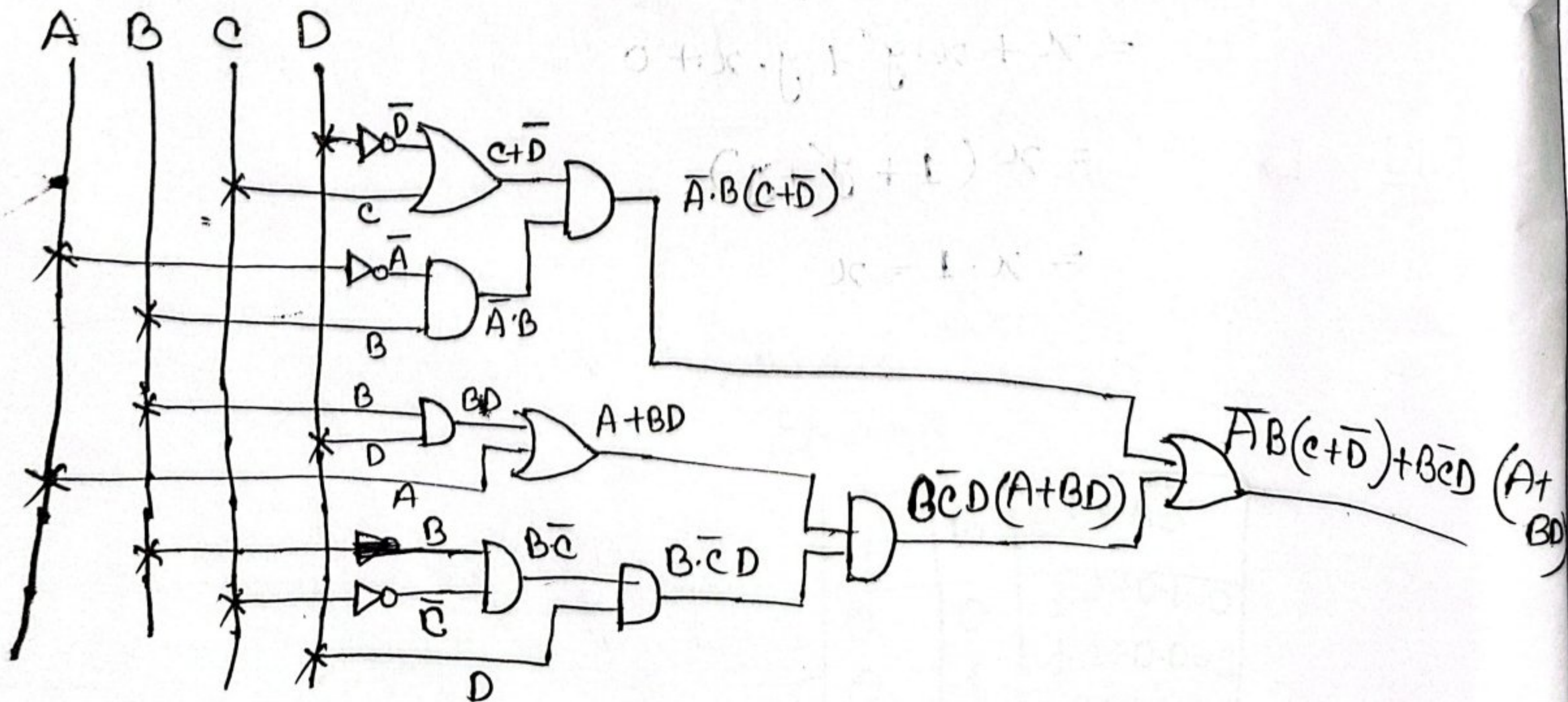
$= (x+y)[x'y + z(x'+y+1)]$

$= (x+y)(x'y + z)$

	B	A
$Y = AB + A\bar{B}$	0	0
$0 = 0 \cdot 0 + 0 \cdot 1$	0	0
$1 = 1 \cdot 0 + 0 \cdot 1$	1	0
$0 = 1 \cdot 0 + 0 \cdot 1$	0	1
$1 = 0 \cdot 0 + 1 \cdot 1$	1	1

$= xz + yz + x'y$

\*  $F(A, B, C, D) = \bar{A}B(C+\bar{D}) + B\bar{C}D(A+BD)$





# # Deriving Boolean function from truth table

A	B	C	F
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

$$F(A, B, C) = \underbrace{\bar{A}\bar{B}\bar{C}}_{\text{Minterm}} + \underbrace{\bar{A}B\bar{C}}_{\text{Minterm}} + \underbrace{A\bar{B}C}_{\text{Minterm}} + \underbrace{ABC}_{\text{Minterm}}$$

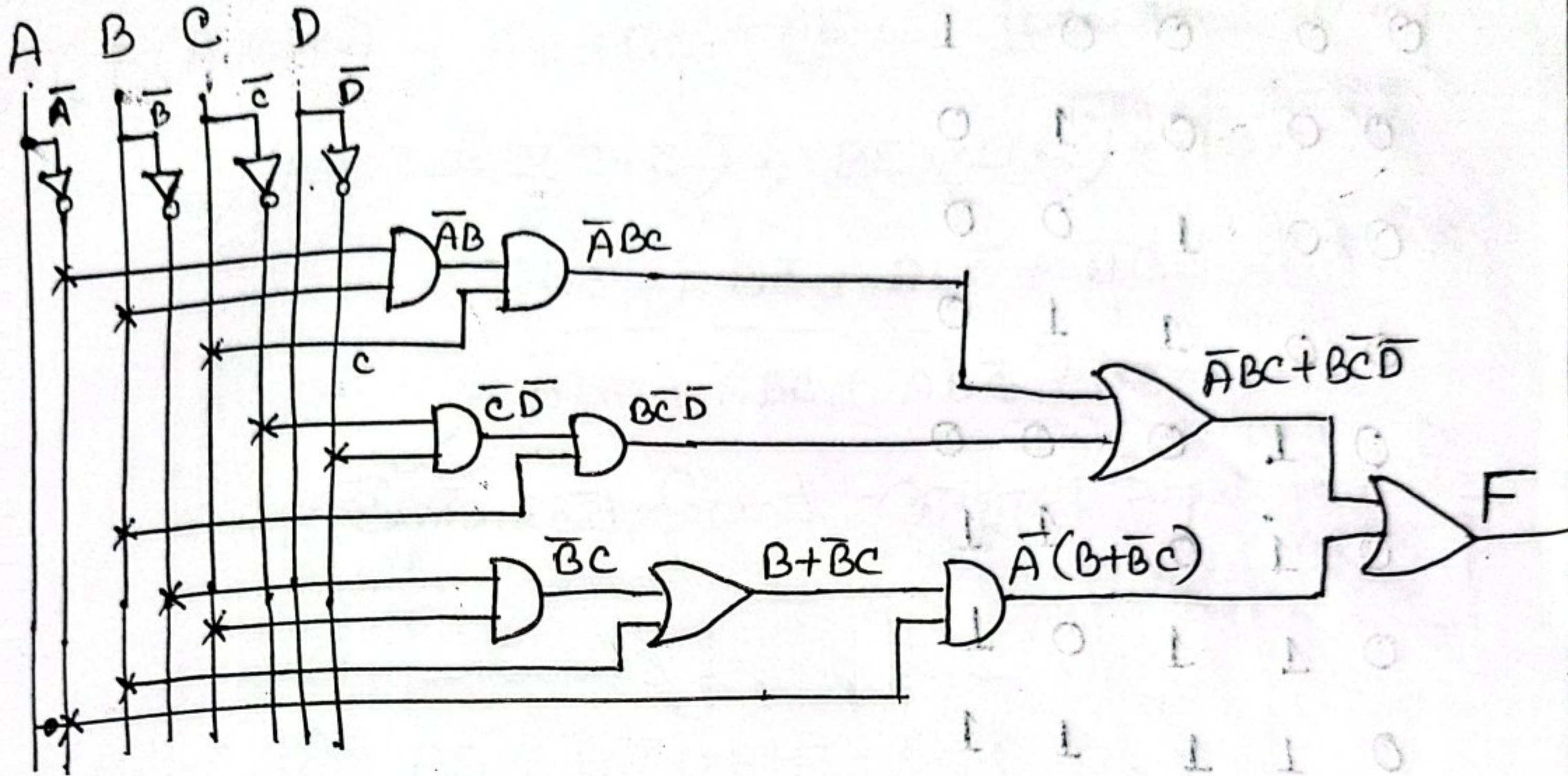
Min term: Min term is the product of input variables or their compliments in such a way that the value of the product is always 1.

- (1) SOP - Sum of Products } Boolean function  
 (2) POS - Product of Sum }

$$* F(A,B,C,D) = \bar{A}BC + B\bar{C}\bar{D} + \bar{A}(B+\bar{B}C)$$

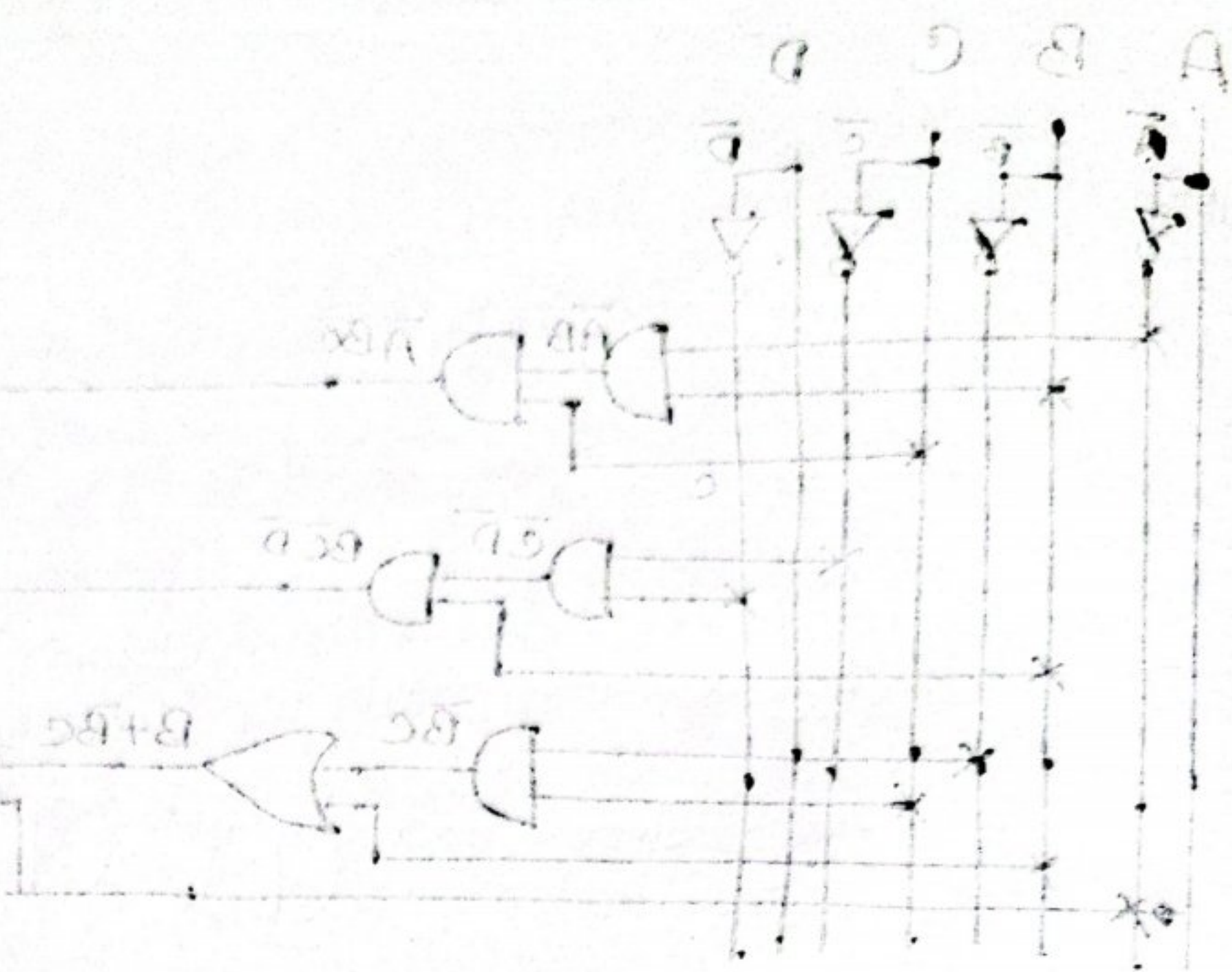
Draw logic diagram

06-02-2024



A	B	C	D	$\bar{A}$	$\bar{B}$	$\bar{C}$	$\bar{D}$	$\bar{A}B$	$B\bar{C}\bar{D}$	$\bar{B}C$	$B+\bar{B}C$	$\bar{A}(B+\bar{B}C)$	F
0	0	0	0	1	1	1	1	0	0	0	0	0	0
0	0	0	1	1	1	1	0	0	0	0	0	0	0
0	0	1	0	1	1	0	1	0	0	1	1	1	1
0	0	1	1	1	1	0	0	0	0	1	1	1	1
0	1	0	0	1	0	1	1	0	1	0	1	1	1
0	1	0	1	1	0	1	0	0	0	0	1	1	1
0	1	1	0	1	0	0	1	1	0	0	1	1	1
0	1	1	1	1	0	0	0	1	0	0	1	1	1
1	0	0	0	0	1	1	1	0	0	0	0	0	0
1	0	0	1	0	1	1	0	0	0	0	0	0	0
1	0	1	0	0	1	0	1	0	0	1	1	0	0
1	0	1	1	0	1	0	0	0	0	1	1	0	0
1	1	0	0	0	0	1	1	0	1	0	1	0	1
1	1	0	1	0	0	1	0	0	0	0	1	0	1
1	1	1	0	0	0	0	1	0	0	0	1	0	1
1	1	1	1	0	0	0	0	0	0	0	1	0	1

A	B	C	D	F
0	0	0	0	1
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1



$$F(A, B, C, D) = \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D$$

Max term: Max term is a summation of all input variables, or their complements in such a way that the value of the summation is always 0.

A	B	C	F
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	1

$$F(A, B, C) = (A+B+C) \cdot (\bar{A}+\bar{B}+\bar{C}) \cdot (\bar{A}+\bar{B}+C)$$

$$\rightarrow \bar{A} + B + \bar{C}$$

$$\rightarrow \bar{A} + \bar{B} + \bar{C}$$

Canonical Format: সম্মানিত ফর্ম

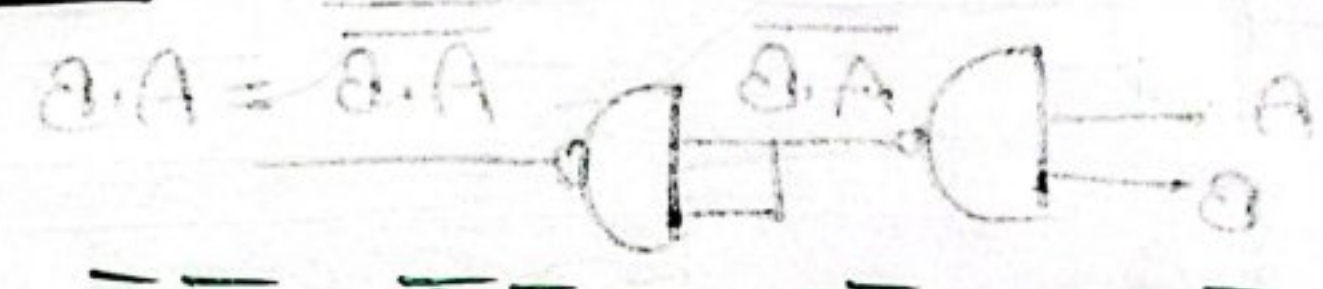
$$F(A, B, C) = \bar{A}B + B\bar{C} + AB C \quad [\text{Standard form}]$$

$$= \bar{A}B(C + \bar{C}) + B\bar{C}(A + \bar{A}) + AB C$$

$$= \bar{A}BC + \bar{A}B\bar{C} + AB\bar{C} + \bar{A}B\bar{C} + AB C$$

$$= \bar{A}BC + \bar{A}B\bar{C} + AB\bar{C} + AB C$$

Canonical format সম্মানিত ফর্ম Input variable সম্মানিত



\*  $F(A, B, C, D) = \bar{A}\bar{B} + \bar{B}\bar{C}D + A\bar{C} + AB\bar{C}$

$$= \bar{A}\bar{B}(C + \bar{C})(D + \bar{D}) + (A + \bar{A})\bar{B}\bar{C}D + A(B + \bar{B})\bar{C}(D + \bar{D})$$

$$+ AB\bar{C}(D + \bar{D})$$

$$= \bar{A}\bar{B}CD + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + A\bar{B}\bar{C}\bar{D}$$

$$+ AB\bar{C}D + AB\bar{C}\bar{D} + AB\bar{C}\bar{D} + AB\bar{C}\bar{D}$$

$$+ AB\bar{C}D + AB\bar{C}\bar{D}$$

$$= \bar{A}\bar{B}CD + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D$$

$$+ AB\bar{C}D + AB\bar{C}\bar{D} + AB\bar{C}\bar{D}$$

# Universality of NAND-NOR

## 1. NAND to NOT

$$Y = \overline{A \cdot B}$$

$$= \overline{A \cdot A} = \overline{A}$$

Same input দিচ্ছি

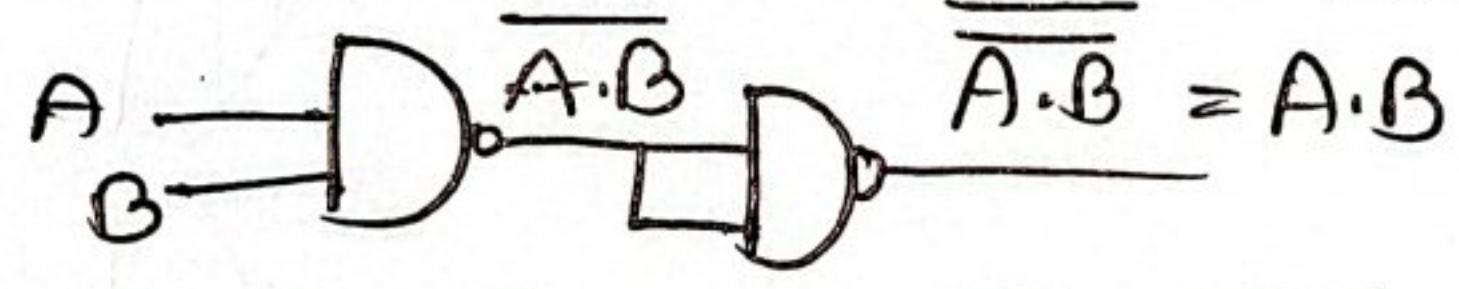
## 2. NAND to AND

$$Y = \overline{\overline{A \cdot B}}$$

$$= \overline{\overline{A \cdot B}}$$

$$= A \cdot B$$

আরেকবার NAND এর entry দিচ্ছি

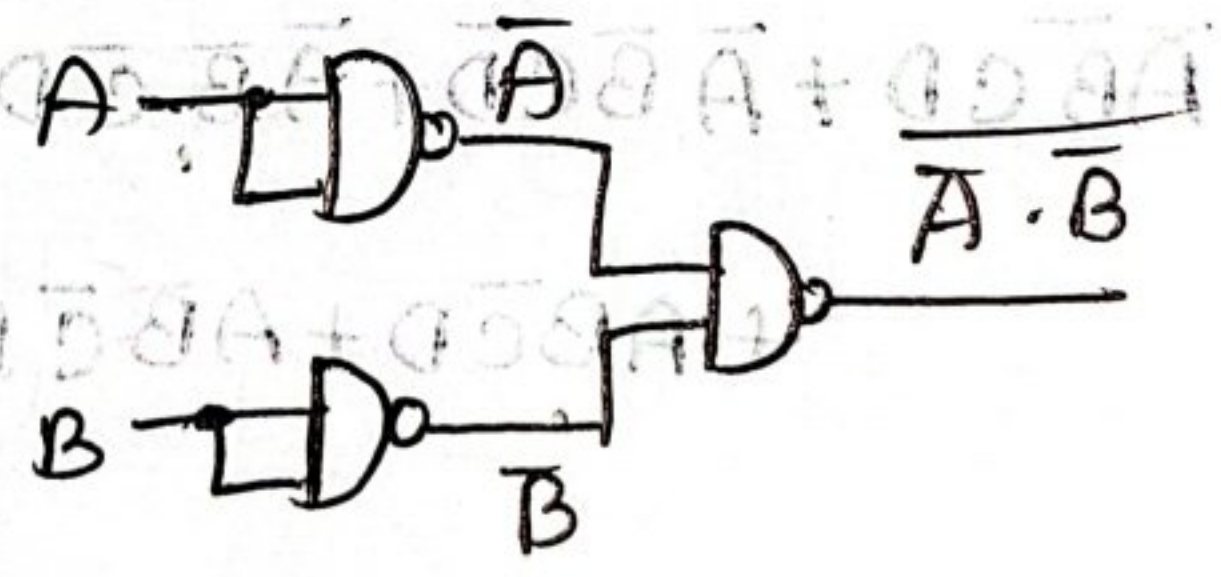


## 3. NAND to OR

$$Y = \overline{\overline{A \cdot B}}$$

$$= \overline{\overline{A} \cdot \overline{B}}$$

$$= A + B$$



$$\overline{\overline{A \cdot B}} = \overline{\overline{A} \cdot \overline{B}} = A + B$$

Q. Implement the following with NAND gates  
 1. NOR TO NOT (eater)

$$Y = \overline{A+B}$$

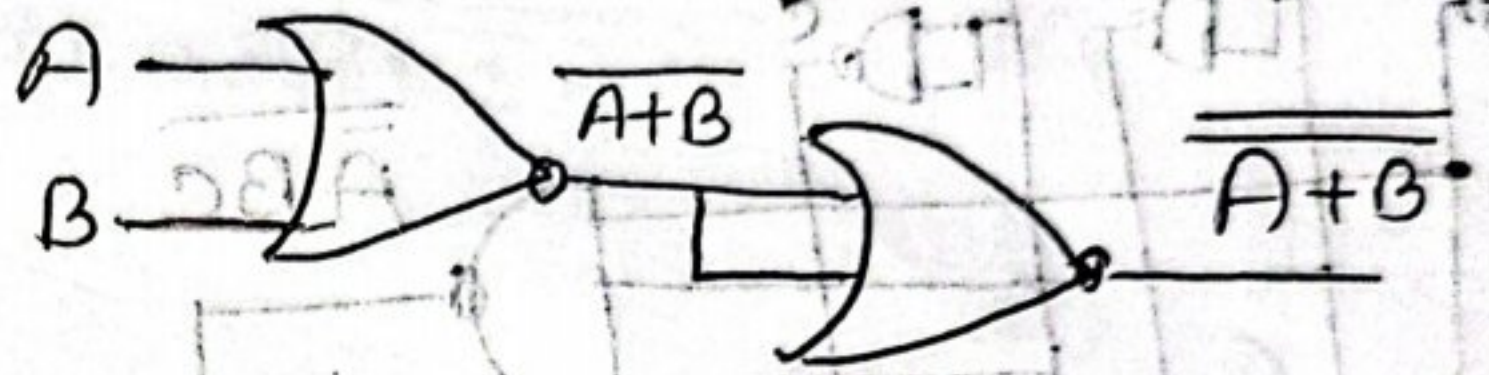
$$= \overline{A+A} = \overline{A}$$



2. NOR TO OR

$$Y = \overline{\overline{A+B}}$$

$$= \overline{\overline{A+B}} = A+B$$

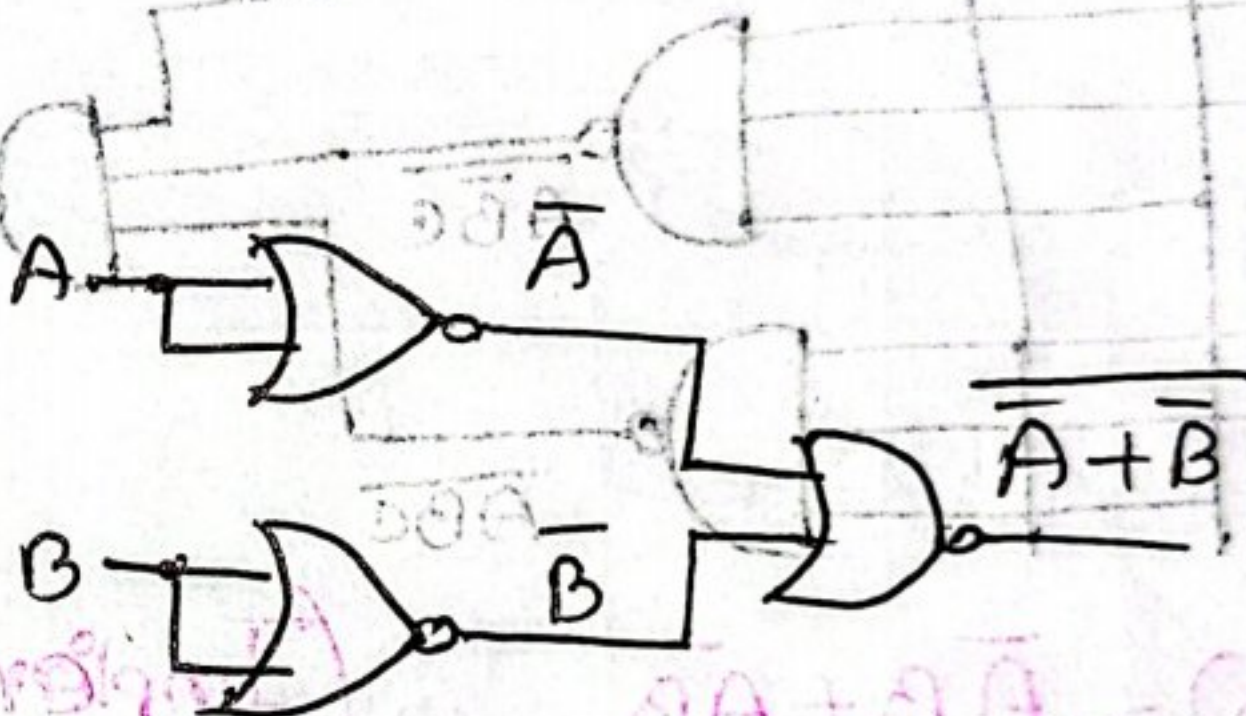


3. NOR TO AND

$$Y = \overline{\overline{A+B}}$$

$$= \overline{\overline{A}} \cdot \overline{\overline{B}}$$

$$= A \cdot B$$



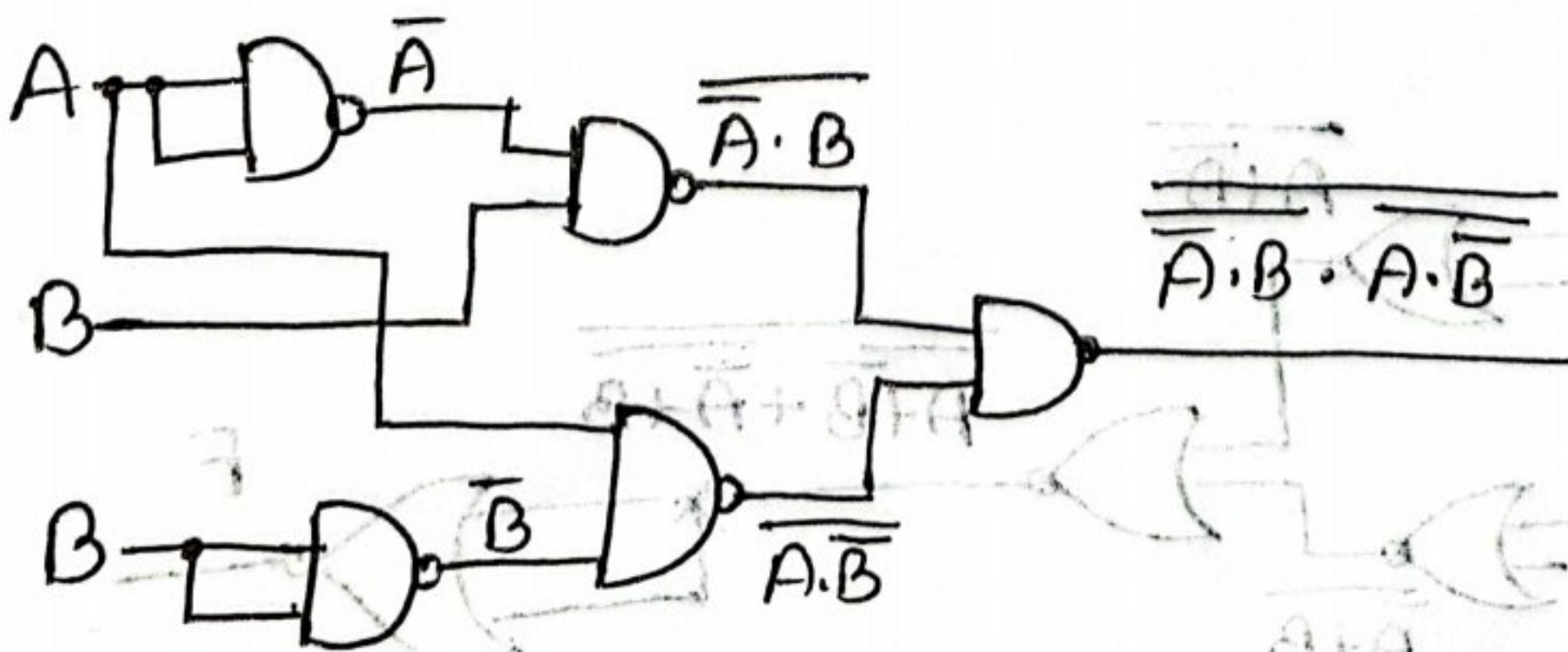
Q. Implement the following with NAND gates

$$F(A,B) = \overline{A}B + A\overline{B}$$

[Implement the function with only NAND Gates]

$$= \overline{\overline{\overline{A}B + A\overline{B}}}$$

$$= \overline{\overline{A}B} \cdot \overline{A\overline{B}}$$

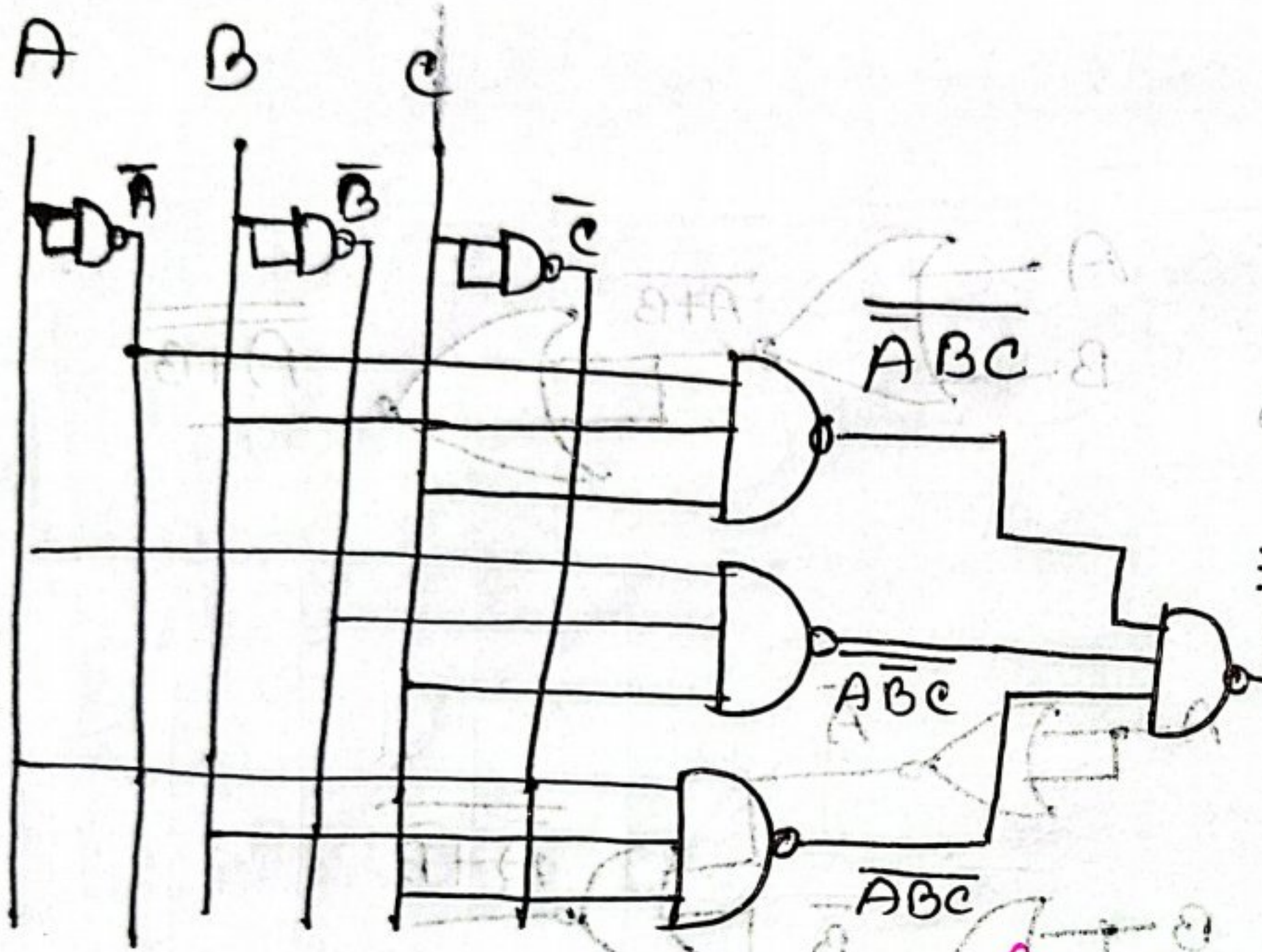


$F(A,B,C) = \bar{A}BC + A\bar{B}C + ABC$

(Implement with NAND Gates)

$$= \overline{\overline{\bar{A}BC} + \overline{A\bar{B}C} + \overline{ABC}}$$

$$= \overline{\bar{A}BC \cdot A\bar{B}C \cdot ABC}$$



\*  $F(A,B) = \bar{A}B + A\bar{B}$

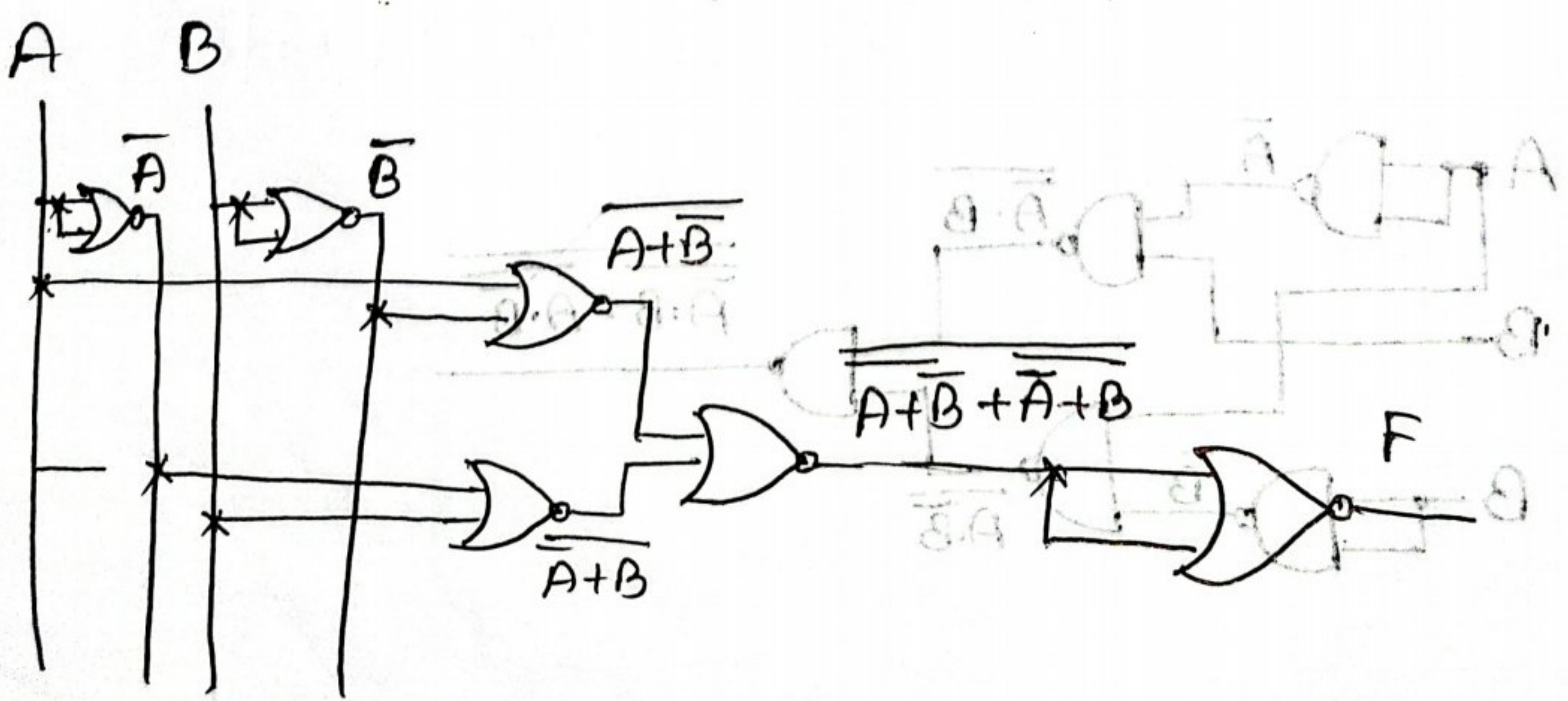
(Implement the function with

Only NOR Gates)

$$= \overline{\overline{\bar{A} \cdot B} + \overline{A \cdot \bar{B}}}$$

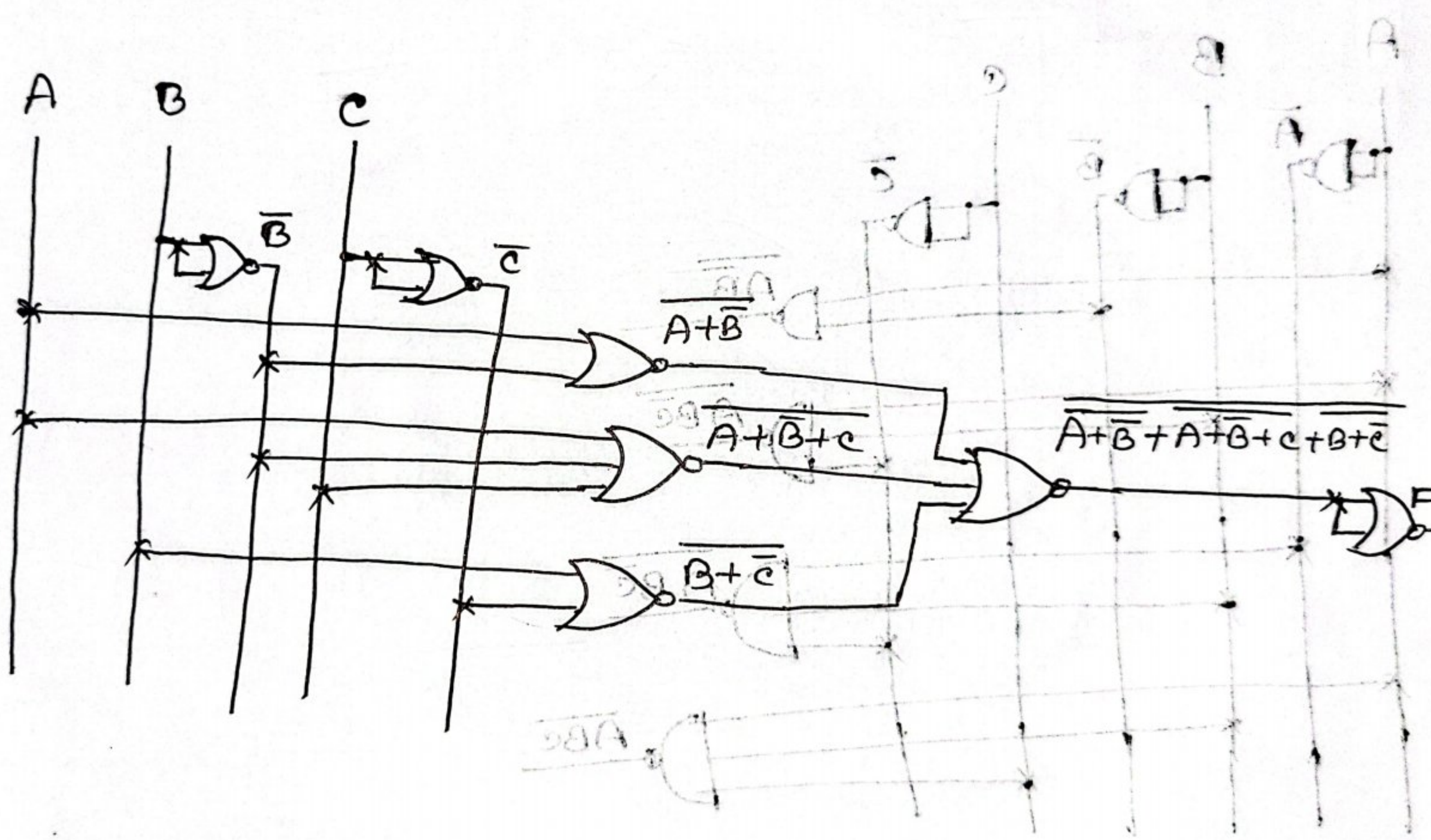
$$= \overline{\bar{A} + \bar{B} + A + \bar{A} + A + \bar{B}}$$

$$= \overline{\bar{A} + \bar{B} + A + B}$$



Ex  $F(A, B, C) = \overline{A}B(B+\overline{C}) + \overline{B}C$  (Implement the function with only NOR Gates)

$$\begin{aligned}
 F &= \overline{A}B + \overline{A}B\overline{C} + \overline{B}C \\
 &= \overline{\overline{\overline{A}B}} + \overline{\overline{\overline{A}B\overline{C}}} + \overline{\overline{\overline{B}C}} \\
 &= \overline{A+B} + \overline{A+B+C} + \overline{B+C} \\
 &= \overline{\overline{A+B} + \overline{A+B+C} + \overline{B+C}}
 \end{aligned}$$



$$F(A, B, C) = A\bar{B}(A+Bc) + B\bar{C}(A+\bar{A}B) + A\bar{B}C(\bar{B}+Ac)$$

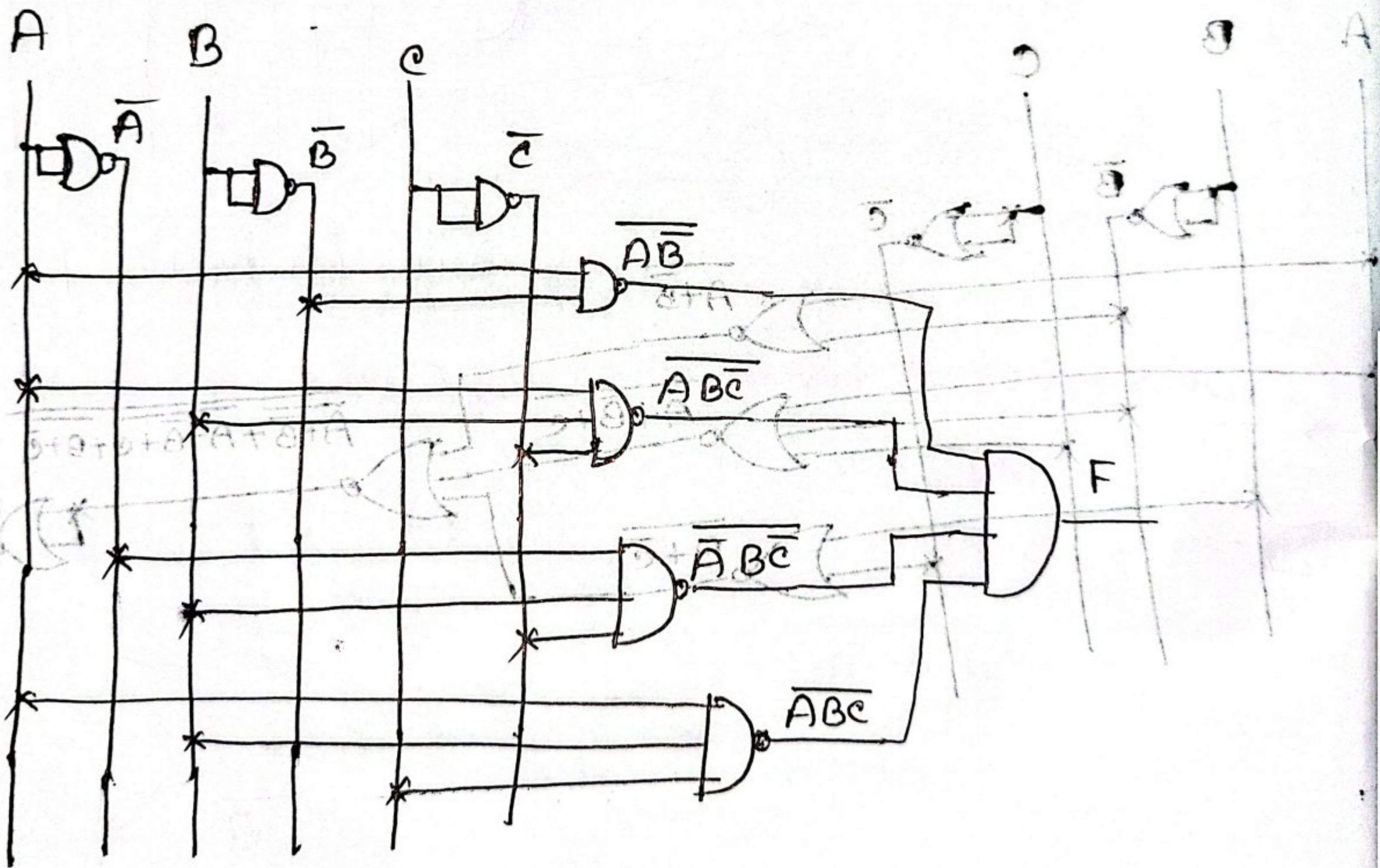
**NAND**

$$= A\bar{B} + A\bar{B}Bc + AB\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{B}C + ABC$$

$$= A\bar{B} + AB\bar{C} + \bar{A}B\bar{C} + ABC$$

$$= \overline{\overline{A\bar{B} + AB\bar{C} + \bar{A}B\bar{C} + ABC}}$$

$$= \overline{\overline{A\bar{B}} \cdot \overline{AB\bar{C}} \cdot \overline{\bar{A}B\bar{C}} \cdot \overline{ABC}} = \overline{\overline{A\bar{B}} \cdot \overline{AB\bar{C}} \cdot \overline{\bar{A}B\bar{C}} \cdot \overline{ABC}}$$

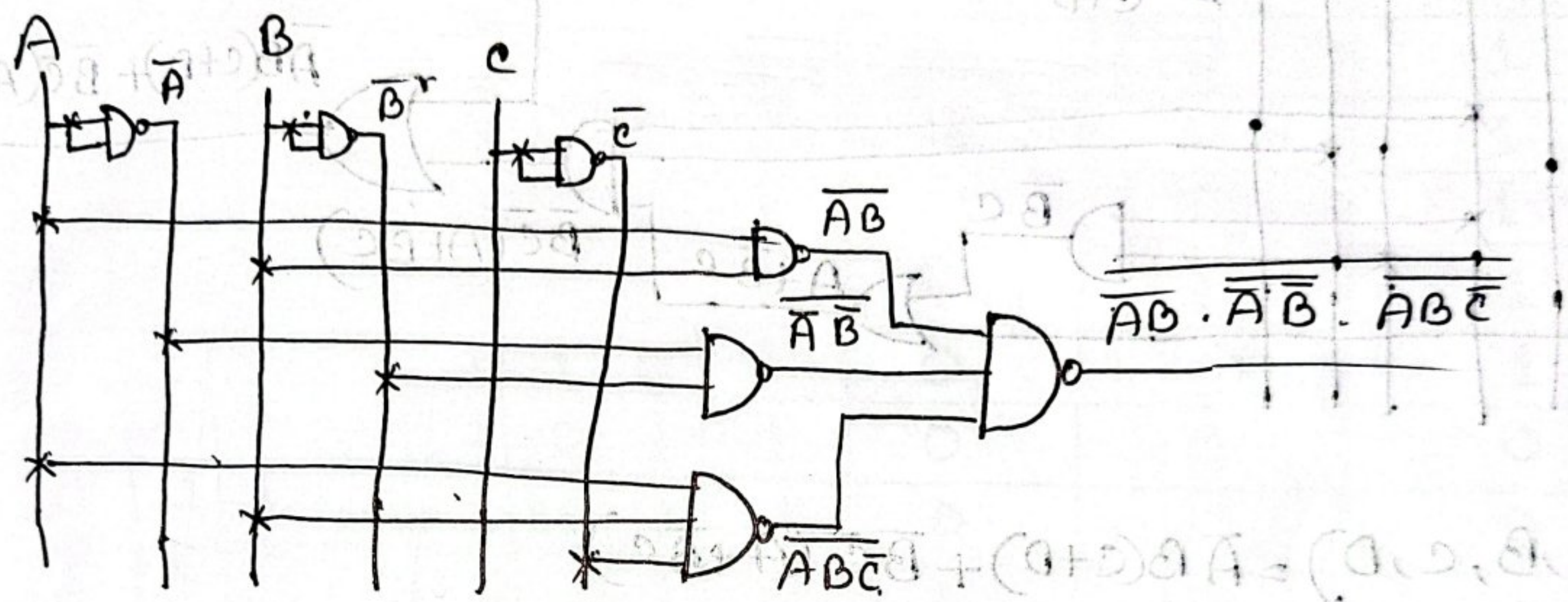


Implement the function with only NAND Gates

$$F(A,B,C) = AB + \bar{A}\bar{B} + ABC\bar{C}$$

$$= \overline{\overline{AB + \bar{A}\bar{B} + ABC\bar{C}}}$$

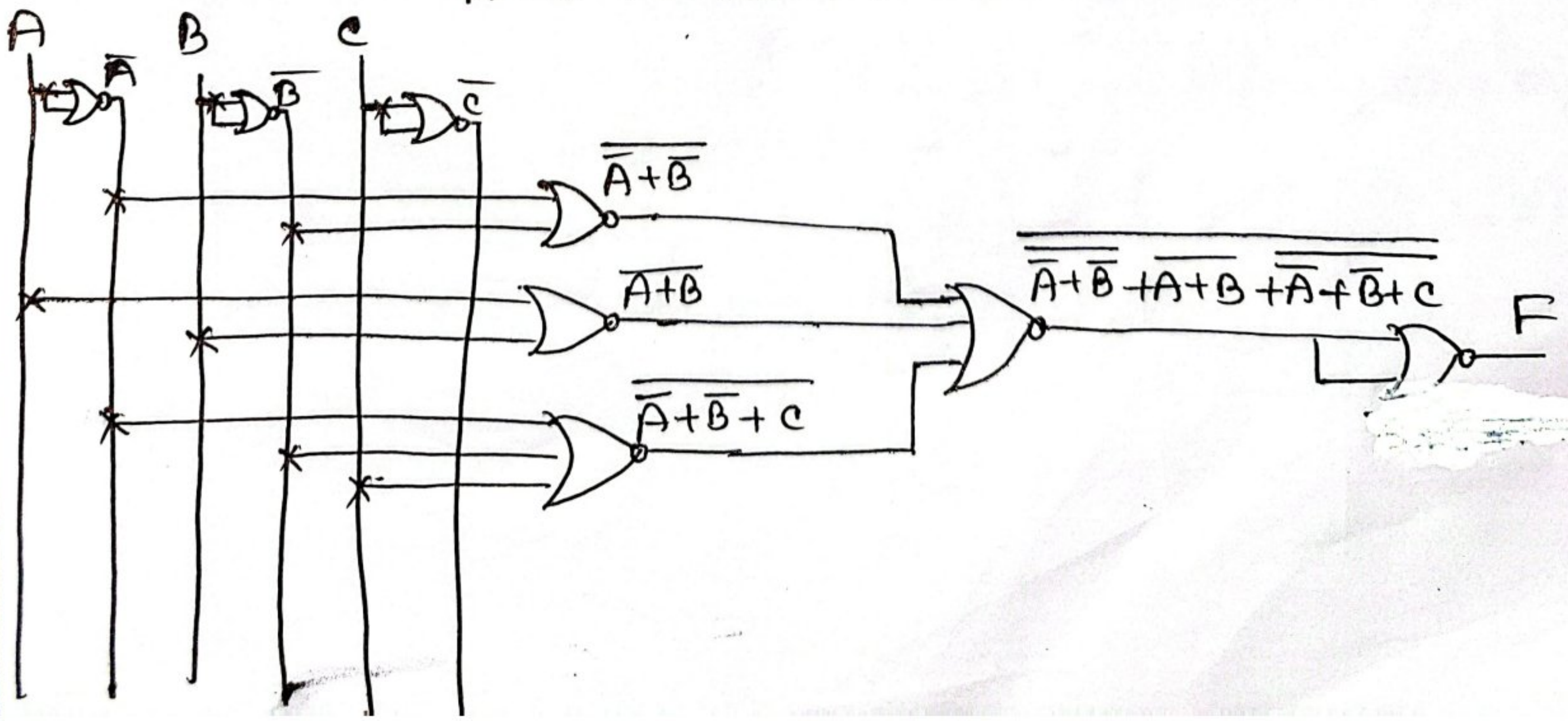
$$= \overline{\overline{AB} \cdot \overline{\bar{A}\bar{B}} \cdot \overline{ABC\bar{C}}}$$



$$F(A,B,C) = AB + \bar{A}\bar{B} + ABC\bar{C}$$

$$= \overline{\overline{AB} + \overline{\bar{A}\bar{B}} + \overline{ABC\bar{C}}}$$

$$= \overline{\overline{A+B} + \overline{A+B} + \overline{A+B+C}}$$



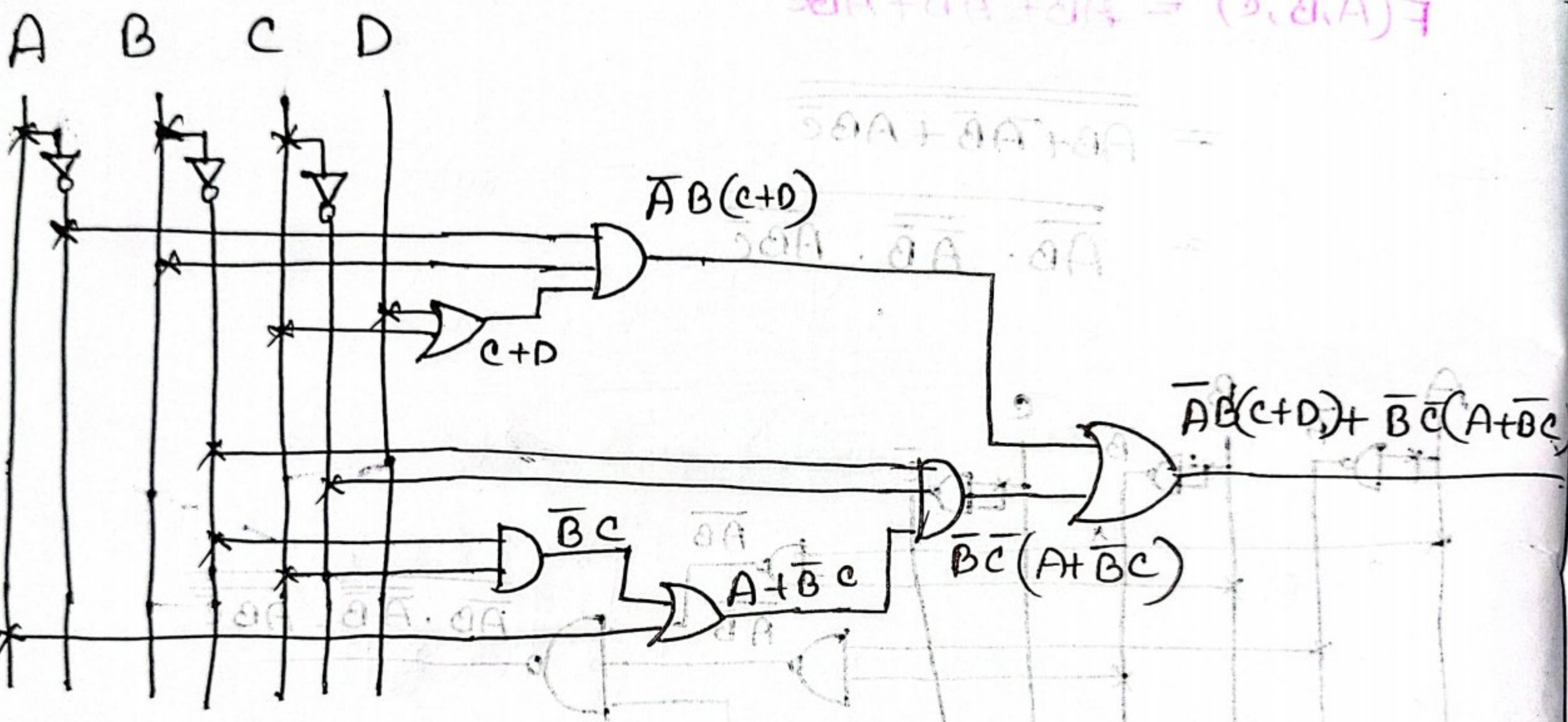
PSQS-50-01

$F(A,B,C,D) = \overline{A}B(C+D) + \overline{B}\overline{C}(A+\overline{B}C)$

$\overline{B}A + B\overline{A} + \overline{B}A = (\overline{B}A) \cdot 2$

$\overline{B}A + \overline{B}A + \overline{B}A =$

$\overline{B}A \cdot \overline{B}A \cdot \overline{B}A =$



$F(A,B,C,D) = \overline{A}B(C+D) + \overline{B}\overline{C}(A+\overline{B}C)$

$= \overline{A}Bc + \overline{A}BD + A\overline{B}\overline{C} + 0$

$\overline{B}A + B\overline{A} + \overline{B}A = (\overline{B}A) \cdot 2$

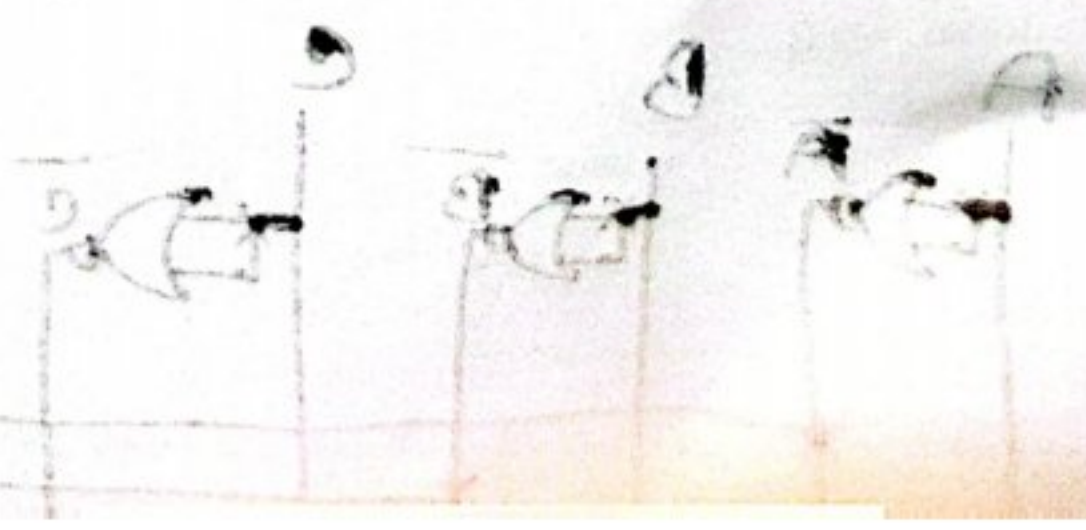
$= \overline{A}B(C+D) + A\overline{B}\overline{C}$

$\overline{B}A + \overline{B}A + \overline{B}A =$

$\overline{B} + \overline{B} + \overline{B} + \overline{B} + \overline{B} + \overline{B} =$

$\overline{B} + \overline{B} + \overline{B} + \overline{B} + \overline{B} + \overline{B} =$

$\overline{B} + \overline{B}$



A	B	C	D	$\bar{A}$	$\bar{B}$	$\bar{C}$	$\bar{D}$	C+D	$\overline{AB(C+D)}$	$\overline{ABC}$	F
0	0	0	0	1	1	1	1	0	0	0	0
0	0	0	1	1	1	1	0	1	0	0	0
0	0	1	0	1	1	0	1	1	0	0	0
0	0	1	1	1	1	0	0	1	0	0	0
0	1	0	0	1	0	1	1	0	0	0	0
0	1	0	1	1	0	1	0	1	1	0	1
0	1	1	0	1	0	0	1	1	1	0	1
0	1	1	1	1	0	0	0	1	1	0	1
1	0	0	0	0	1	1	1	0	0	1	1
1	0	0	1	0	1	1	0	1	0	1	1
1	0	1	0	0	1	0	1	1	0	0	0
1	0	1	1	0	1	0	0	1	0	0	0
1	1	0	0	0	0	1	1	0	0	0	0
1	1	0	1	0	0	1	0	1	0	0	0
1	1	1	0	0	0	0	1	1	0	0	0
1	1	1	1	0	0	0	0	1	0	0	0

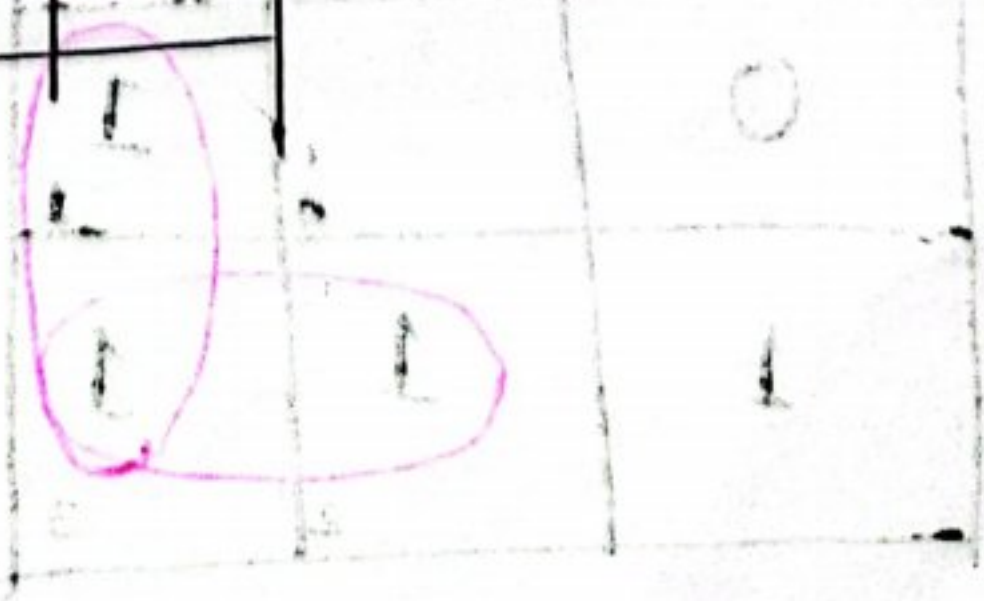


A	B	F	Min term	Max term
0	0	1	$\bar{A}\bar{B}$ $m_0$	$M_0$
0	1	1	$\bar{A}B$ $m_1$	$M_1$
1	0	1	$A\bar{B}$ $m_2$	$M_2$
1	1	0	$AB$ $m_3$	$M_3$

$$F(A, B) = \bar{A}\bar{B} + \bar{A}B + A\bar{B}$$

$$= m_0 + m_1 + m_2$$

$$= \sum m(0, 1, 2)$$



# DLD minimization technique

18-02-2024

\* Implement the boolean function using only NAND gates

Gates

$$F(x, y, z) = \sum_m (1, 2, 3, 6, 7)$$

$$= \bar{x}\bar{y}z + \bar{x}y\bar{z} + \bar{x}yz + x\bar{y}\bar{z} + xyz$$

$$= \overline{\bar{x}\bar{y}z} \cdot \overline{\bar{x}y\bar{z}} \cdot \overline{\bar{x}yz} \cdot \overline{x\bar{y}\bar{z}} \cdot \overline{xyz}$$

\*  $F(x, y) = \bar{x}y + x\bar{y} + xy$

$$= y(x + \bar{x}) + x\bar{y}$$

$$= y + x\bar{y}$$

$$= (y + x) \cdot (y + \bar{y})$$

$$= x + y$$

## K-Map

(Karnaugh)

$$\bar{A}A + A\bar{A} + B\bar{B} + B\bar{B} = 0$$

$$F(x, y) = \bar{x}y + x\bar{y} + xy = y + x\bar{y}$$

		F	B	A
		1	0	0
		1	1	0
		1	1	1

	$\bar{x}$	$x$
$\bar{y}$	0	1
$y$	1	1

Group 1:  $\bar{y}$  (circled)  
Group 2:  $x$  (circled)  
Group 3:  $x\bar{y}$  (circled)

- Group element
- Pair, Quad, Octate
  - Minimum number of Groups but max size of groups

\*  $F(A,B,C) = \sum m(0,2,3,4,5,7)$

$= \bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + \bar{A}BC + A\bar{B}\bar{C} + A\bar{B}C + ABC$

Stray Code

$= \bar{A}\bar{C} + BC + \bar{A}B$

		C	0	1
AB	00	1		
01	1		1	
11			1	
10	1		1	

\*  $F(A,B,C,D) = \sum m(2,4,6,8,9,10,12,15)$

$= \bar{A}\bar{B}C\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}BC\bar{D} + A\bar{B}\bar{C}\bar{D} + A\bar{B}C\bar{D} + A\bar{B}C\bar{D} + ABC\bar{D} + ABCD$

$= \bar{A}C\bar{D} + B\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C} + \bar{A}B\bar{D} + ABCD$

		CD	00	01	11	10
AB	00					1
01	1					1
11				1		
10	1	1				1

\*  $F(A, B, C, D) = (0, 1, 2, 4, 6, 8, 10, 12, 14, 15)$  \*  $F(A, B, C, D)$

8 4 2 1  $\bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}BC\bar{D} + \bar{A}B\bar{C}D + \bar{A}BCD + \bar{A}B\bar{C}D + \bar{A}BCD$

$= \bar{A}\bar{B}\bar{C} + \bar{A}BC + \bar{D}$

		$\bar{C}\bar{D}$	$\bar{C}D$	$CD$	$C\bar{D}$
$\bar{A}\bar{B}$	$00$	$01$	$11$	$10$	
$\bar{A}B$	$00$	$01$	$11$	$10$	
$A\bar{B}$	$01$	$01$	$11$	$10$	
$AB$	$11$	$11$	$11$	$10$	
$AB$	$00$	$01$	$11$	$10$	

		$\bar{C}\bar{D}$	$\bar{C}D$	$CD$	$C\bar{D}$
$\bar{A}\bar{B}$	$00$	$01$	$11$	$10$	
$\bar{A}B$	$00$	$01$	$11$	$10$	
$A\bar{B}$	$01$	$01$	$11$	$10$	
$AB$	$11$	$11$	$11$	$10$	

K-map

\*  $F(A,B,c,D) = \sum_m(0,1,2,4,6,8,9,10)$

$= \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + \bar{A}B\bar{C}\bar{D}$

		$\bar{c}\bar{d}$	$\bar{c}d$	$cd$	$c\bar{d}$
$\bar{A}\bar{B}$	00	1	1		1
$\bar{A}B$	01	1			1
$A\bar{B}$	10	1	1		1
$AB$	11				

$= \bar{B}\bar{C} + \bar{A}\bar{D} + \bar{B}\bar{D}$

\*  $F(A,B,c,D) = \sum_m(1,4,8,9,10,11,12,14)$

$= \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D$

		$\bar{c}\bar{d}$	$\bar{c}d$	$cd$	$c\bar{d}$
$\bar{A}\bar{B}$	00		1		
$\bar{A}B$	01	1			
$A\bar{B}$	11	1			1
$AB$	10	1	1	1	1

$= \bar{A}\bar{B} + \bar{A}\bar{D} + \bar{B}\bar{C}D + \bar{B}\bar{C}\bar{D}$

# Don't Care Condition

K-map

\*  $F(A,B,C,D) = \sum_m (0,1,2,3,6,7,9,12) + \sum_d (4,5,8,13,14)$

AB \ CD	$\bar{c}\bar{d}$	$\bar{c}d$	$c\bar{d}$	$cd$
$\bar{A}\bar{B}$ 00	1	1	1	1
$\bar{A}B$ 01	X		1	1
$AB$ 11	1	X		X
$A\bar{B}$ 10	X	1		

$= \bar{A}C + \bar{C}\bar{D} + B\bar{C}$

\*  $F(A,B,C,D) = \sum_m (0,2,5,8,10,12) + \sum_d (3,4,7,11,13,14)$

AB \ CD	$\bar{c}\bar{d}$	$\bar{c}d$	$c\bar{d}$	$cd$
$\bar{A}\bar{B}$ 00	1		X	1
$\bar{A}B$ 01	X	1	X	
$AB$ 11	1	X		X
$A\bar{B}$ 10	1		X	1

$= \bar{B}\bar{D} + B\bar{C}$

# Combinational Logic Circuit

Combinational logic circuit is a circuit that produces output depending on the present values of input variables.

- ① Understanding the problem.
- ② Number of input variables.
- ③ Truth table
- ④ Finding the boolean function
- ⑤ Simplifying the boolean function
- ⑥ Logic diagram.

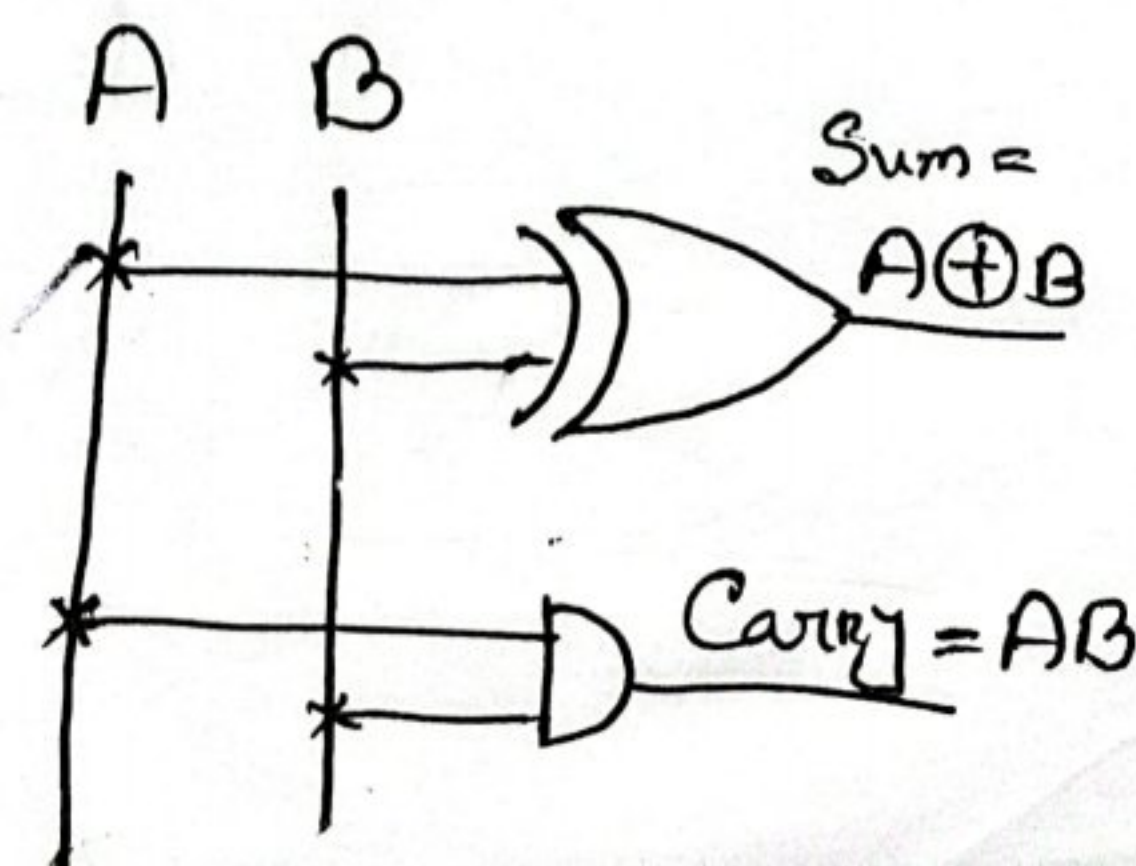
0	1	1	0	0
0	1	0	1	0
1	0	1	1	0
1	0	0	0	1
1	1	0	1	1
1	1	1	1	1

## \* Half Adder

A	B	Sum	Carry
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

$$\text{Sum} = \bar{A}B + A\bar{B} = A \oplus B$$

$$\text{Carry} = AB$$



# (3 bit binary adder (Full Adder))

\* Full adder

two input signals

A	B	C <sub>in</sub>	Sum	C <sub>out</sub>
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

truth table  
 understanding the logic  
 numbers of input variables  
 output of the logic  
 truth table  
 finding the boolean expression  
 simplifying the boolean expression

$$\text{Sum} = \bar{A}\bar{B}C_{in} + \bar{A}B\bar{C}_{in} + A\bar{B}\bar{C}_{in} + ABC_{in}$$

Half Adder

$$C_{out} = \bar{A}B C_{in} + A\bar{B} C_{in} + AB\bar{C}_{in} + ABC_{in}$$

A	B	C <sub>in</sub>	C <sub>out</sub>
0	0	0	0
0	1	1	0
1	0	1	0
1	1	1	1

$$A \oplus B = \bar{A}B + A\bar{B}$$

27-02-2024

\*  $F(w, x, y, z) = \sum_m(0, 2, 4, 5, 6, 7, 8, 10, 13, 15) + \sum_d(11, 12, 14)$

① Simplify the <sup>boolean</sup> function using K-map.

$= \bar{z} + x$

		$\bar{y}z$	$y\bar{z}$	$yz$	$\bar{y}\bar{z}$
$wx \backslash yz$	00	01	11	10	
$\bar{w}\bar{x}$	00	1			1
$\bar{w}x$	01	1	1	1	1
$wx$	11	X	1	1	X
$w\bar{x}$	10	1		X	1

\* Full Adder

A	B	C <sub>in</sub>	Sum	C <sub>out</sub>
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

$$\text{Sum} = \bar{A}\bar{B}C_{in} + \bar{A}B\bar{C}_{in} + A\bar{B}\bar{C}_{in} + ABC_{in}$$

$$\text{Cout} = \bar{A}BC_{in} + A\bar{B}C_{in} + AB\bar{C}_{in} + ABC_{in}$$

$$\text{Sum} = \bar{A}\bar{B}C_{in} + \bar{A}B\bar{C}_{in} + A\bar{B}\bar{C}_{in} + ABC_{in}$$

$$= \bar{A}(\bar{B}C_{in} + B\bar{C}_{in}) + A(\bar{B}\bar{C}_{in} + BC_{in})$$

$$= \bar{A}(B \oplus C_{in}) + A(\overline{B \oplus C_{in}})$$

$$= A \oplus (B \oplus C_{in})$$

$$= A \oplus B \oplus C_{in}$$

$$C_{out} = \bar{A}B C_{in} + A\bar{B}C_{in} + AB\bar{C}_{in} + ABC_{in}$$

$$= C_{in}(\bar{A}B + A\bar{B}) + AB(\bar{C}_{in} + C_{in})$$

$$= C_{in}(A \oplus B) + AB \cdot 1$$

$$= C_{in}(A \oplus B) + AB$$

A	B	C <sub>in</sub>	Sum	C <sub>out</sub>
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

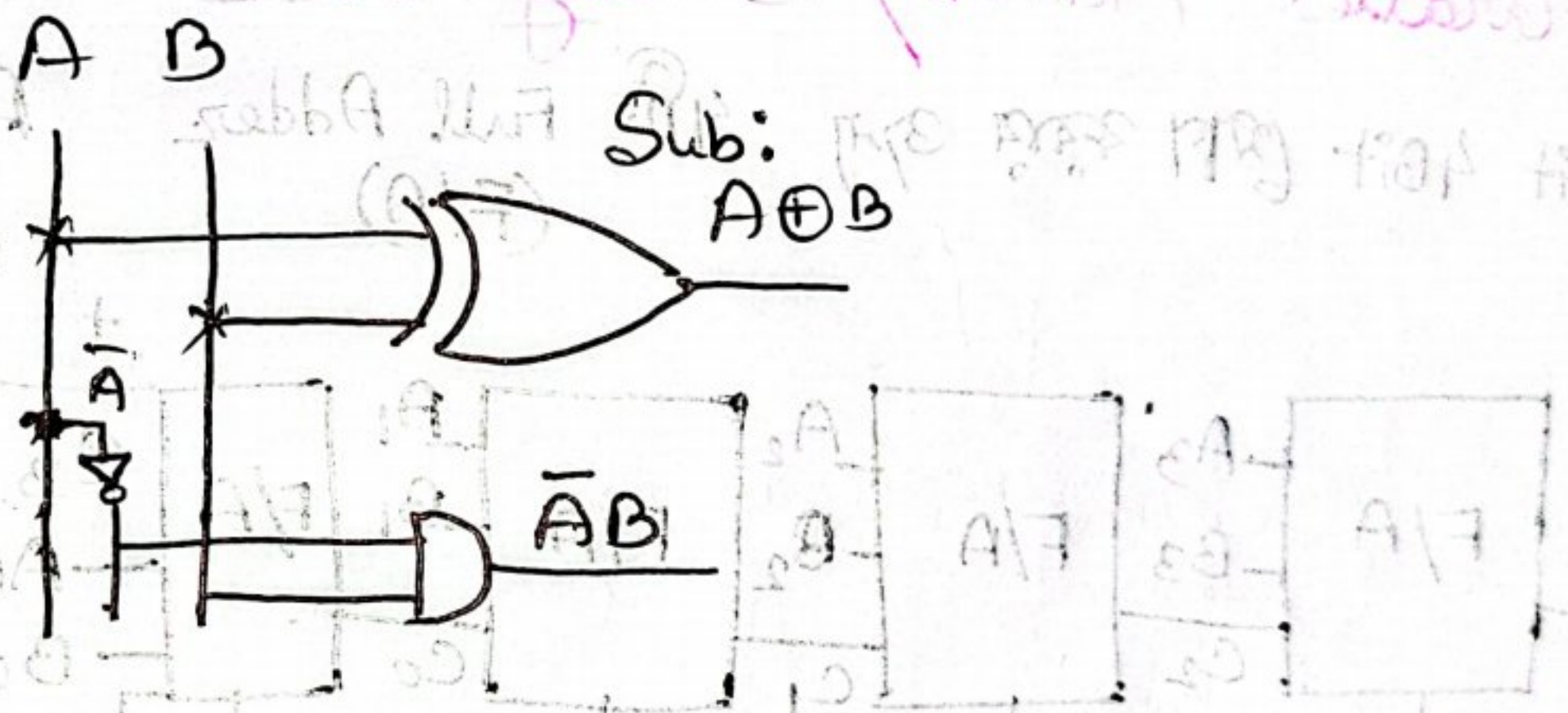
# Half Subtractor

A	B	Sub	Borrow
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

$$\text{Sub} = \bar{A}B + A\bar{B}$$

$$\text{Borrow} = A\bar{B}$$

$$\text{Borrow} = \bar{A}B$$



# Full Subtractor

A	B	Cin	Sub	Borrow
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

$$\text{Sub} = \bar{A}\bar{B}C_{in}$$

$$+ \bar{A}B\bar{C}_{in} + A\bar{B}\bar{C}_{in} + ABC_{in}$$

$$\text{Borrow} = \bar{A}\bar{B}C_{in}$$

$$+ \bar{A}B\bar{C}_{in} + A\bar{B}C_{in} + ABC_{in}$$

$$Sub = \bar{A}\bar{B}C_{in} + \bar{A}B\bar{C}_{in} + A\bar{B}C_{in} + ABC_{in}$$

$$= \bar{A}(B \oplus C_{in}) + A(\overline{B \oplus C_{in}})$$

$$= A \oplus B \oplus C_{in}$$

$$Borrow = \bar{A}\bar{B}C_{in} + \bar{A}B\bar{C}_{in} + \bar{A}BC_{in} + ABC_{in}$$

$$= C_{in}(\bar{A}\bar{B} + AB) + \bar{A}B(\bar{C}_{in} + C_{in})$$

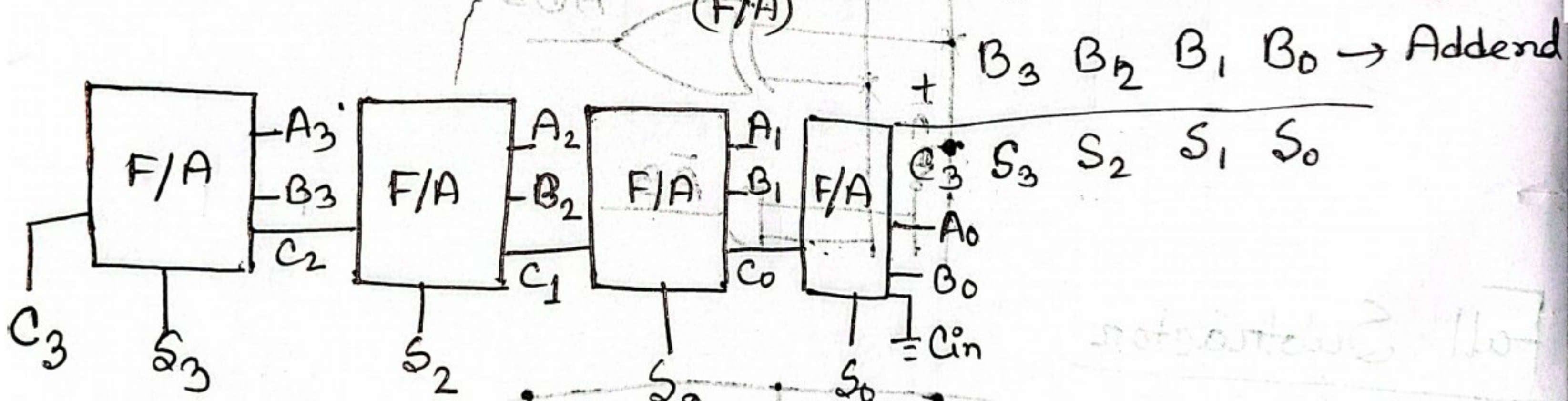
$$= C_{in}(\overline{A \oplus B}) + \bar{A}B$$

	$C_{in}$	$B$	$A$
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0

03-03-2024

## Parallel Adder / Binary Adder

4 Bit 4 Bit (प्रति संख्या अर्थ) 4 Full Adder (F/A)



$c_1$   $c_0$   $c_{in}$   
 $A_3$   $A_2$   $A_1$   $A_0 \rightarrow$  Augend  
 $B_3$   $B_2$   $B_1$   $B_0 \rightarrow$  Addend

$$S_0 = A_0 \oplus B_0 \oplus C_{in}$$

$$C_0 = C_{in}(A_0 \oplus B_0) + A_0 B_0$$

$$S_1 = A_1 \oplus B_1 \oplus C_0$$

$$C_1 = C_0(A_1 \oplus B_1) + A_1 B_1$$

$$S_2 = A_2 \oplus B_2 \oplus C_1$$

$$C_2 = C_1(A_2 \oplus B_2) + A_2 B_2$$

$$S_3 = A_3 \oplus B_3 \oplus C_2$$

$$C_3 = C_2(A_3 \oplus B_3) + A_3 B_3$$

	$C_{in}$	$B$	$A$
0	0	0	0
0	0	1	0
0	1	0	0
0	1	0	1
0	1	1	0
0	1	1	1

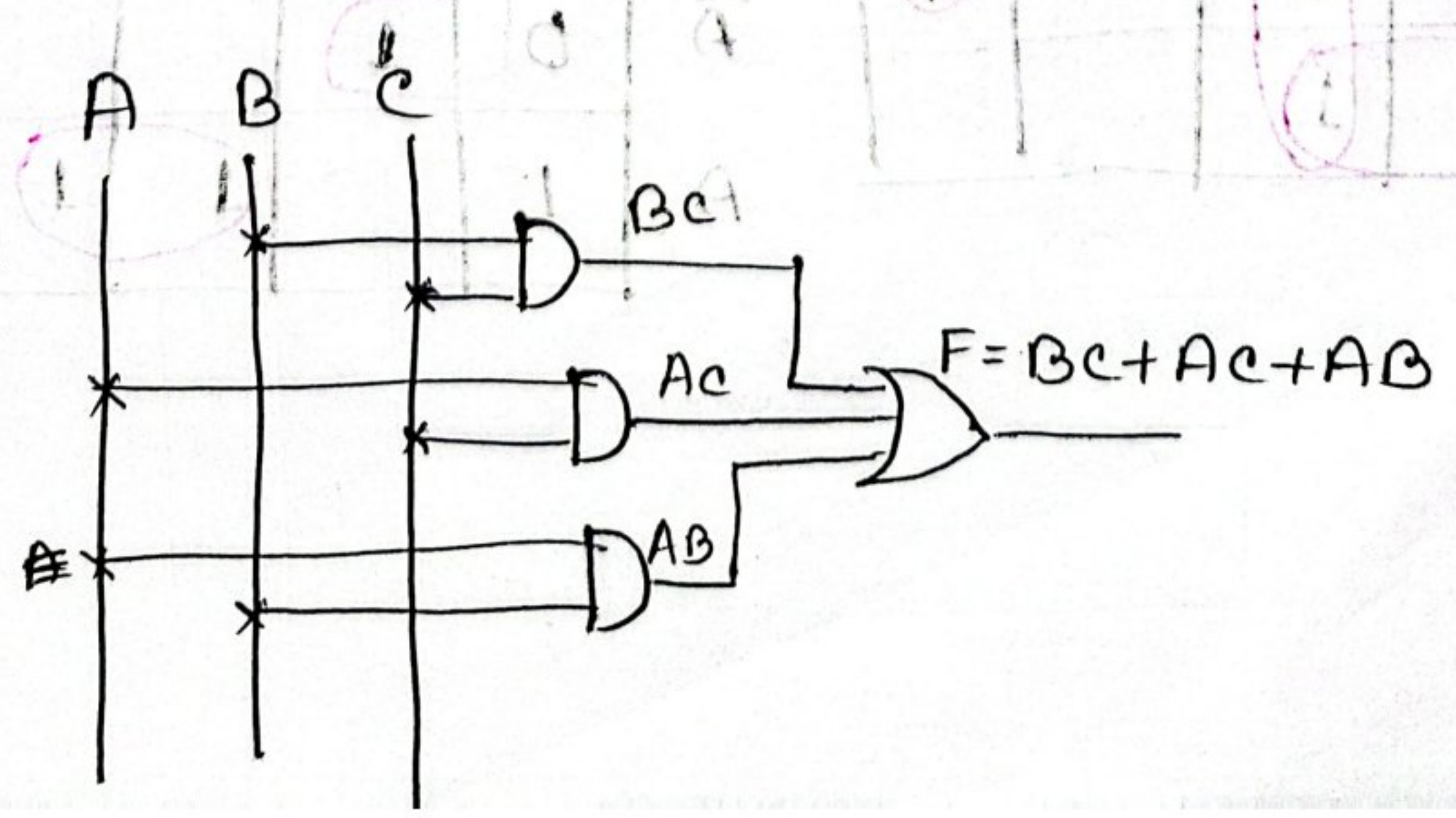
\* Design a combinational Logic Circuit with 3 input and 1 output. The output is 1 when the inputs have more 1's than zeros.

A	B	C	F
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

$$F = \bar{A}B\bar{C} + A\bar{B}C + AB\bar{C} + ABC$$

A \ BC	00	01	11	10
0			1	
1		1	1	1

$$F = BC + AC + AB$$



\* Design a combinational logic circuit with 3 inputs and 3 outputs. When the binary input is 0, 1, 2, 3, the output is one greater than the input. When the input is 4, 5, 6, 7, the output is 2 less than input.

$$X = \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}C = \bar{B}C + A\bar{B}$$

$$Y = \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}C = \bar{A}\bar{B} + \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}C$$

$$Z = \bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}C = \bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}C$$

$$X = \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}C = \bar{B}C + A\bar{B}$$

		$\bar{B}\bar{C}$	$\bar{B}C$	$BC$	$B\bar{C}$
$\bar{A}$	$A$				
		00	01	11	10
0	1	0	1	1	1

$$Z = \bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C} = \bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C} = \bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C}$$

$$Z = \bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C} = \bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C}$$

		$\bar{B}\bar{C}$	$\bar{B}C$	$BC$	$B\bar{C}$
$\bar{A}$	$A$				
		00	01	11	10
0	1	1	1	1	1

$$Y = \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}C = \bar{A}\bar{B} + \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}C$$

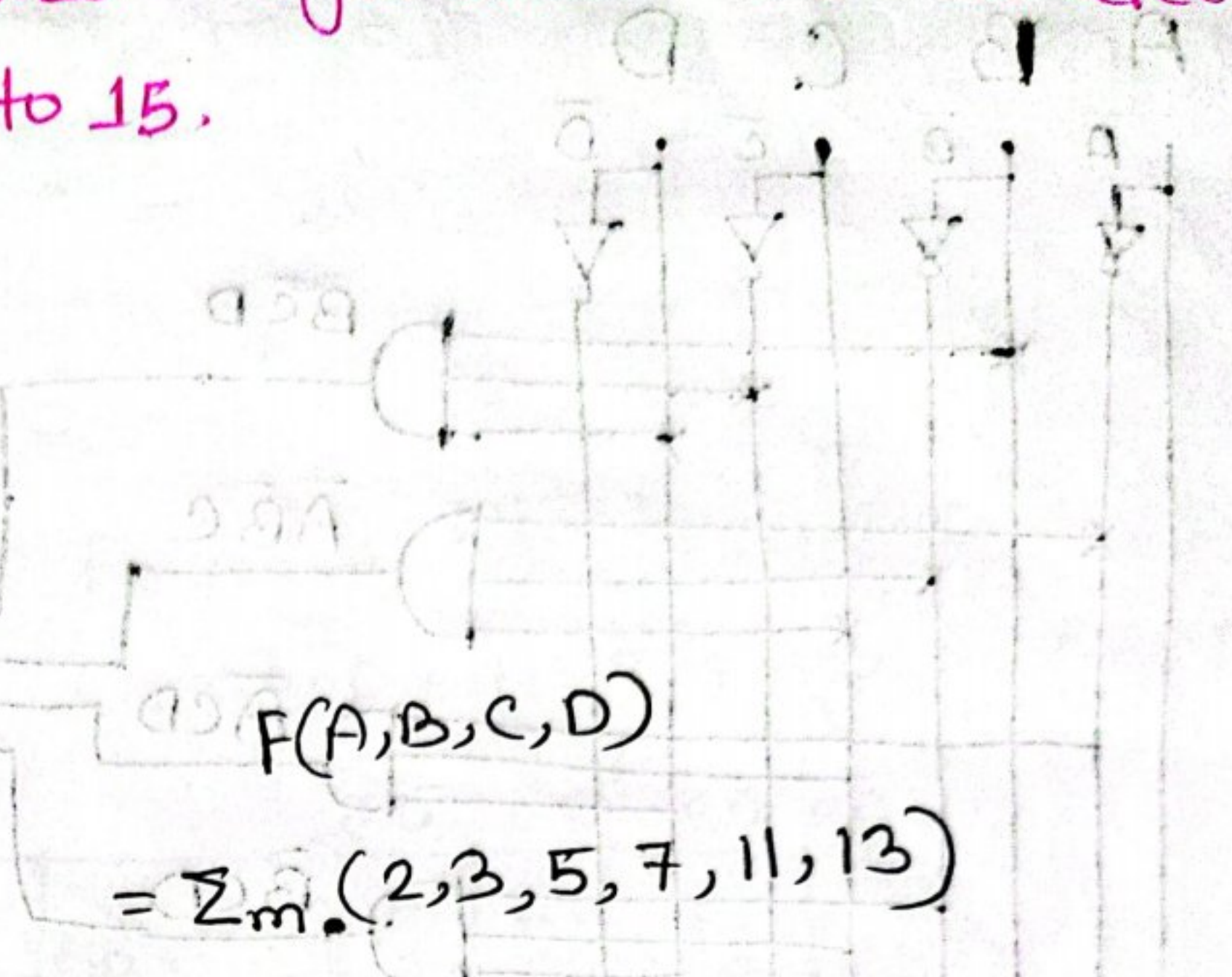
		$\bar{B}\bar{C}$	$\bar{B}C$	$BC$	$B\bar{C}$
$\bar{A}$	$A$				
		00	01	11	10
0	1	0	1	1	1

$$Z = \bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}C = \bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}C$$



\* Design a combinational logic circuit that can detect a prime number up to 15.

A	B	C	D	F
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	0



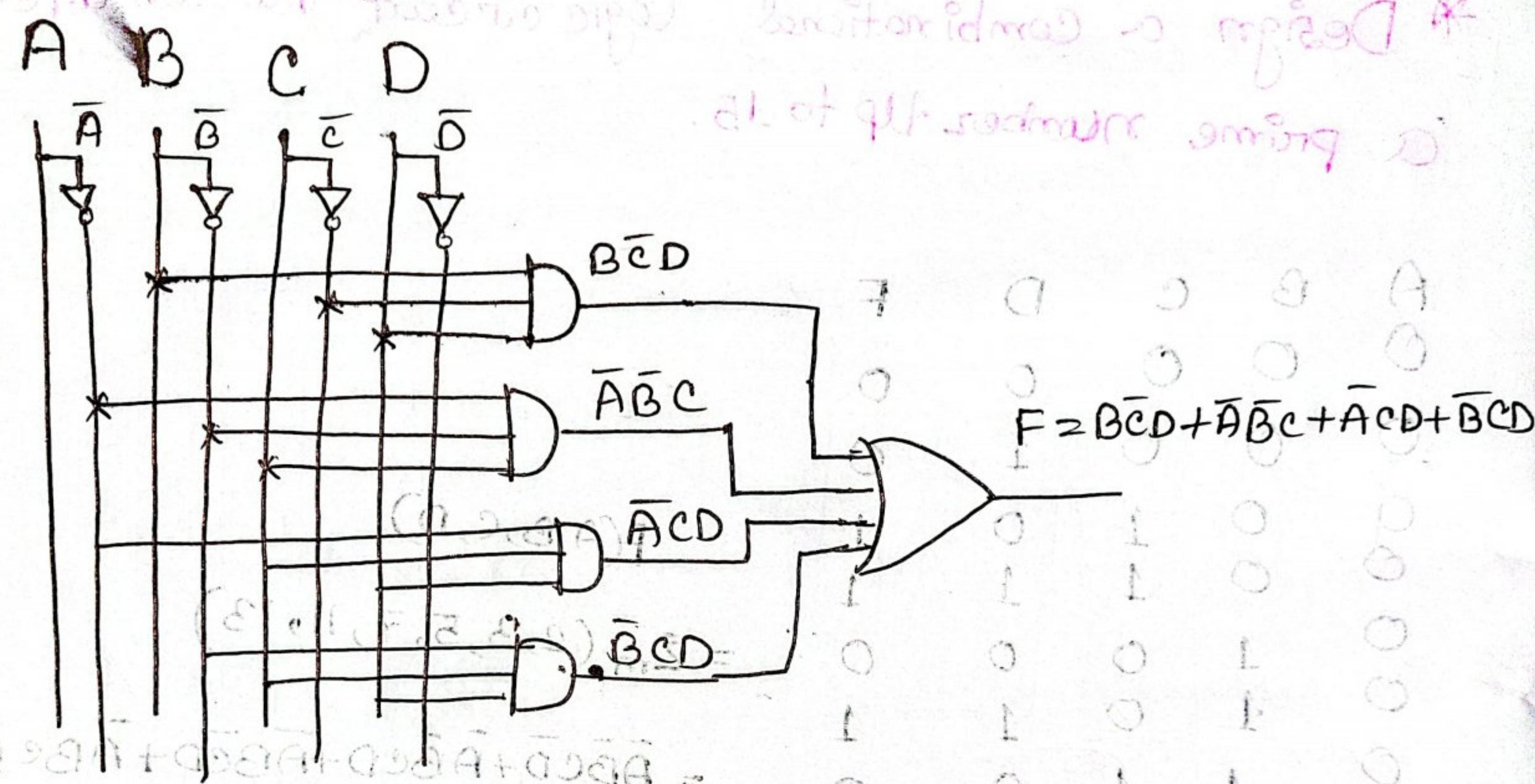
$$F(A, B, C, D) = \sum m(2, 3, 5, 7, 11, 13)$$

$$= \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D + \bar{A}BC\bar{D} + \bar{A}BCD$$

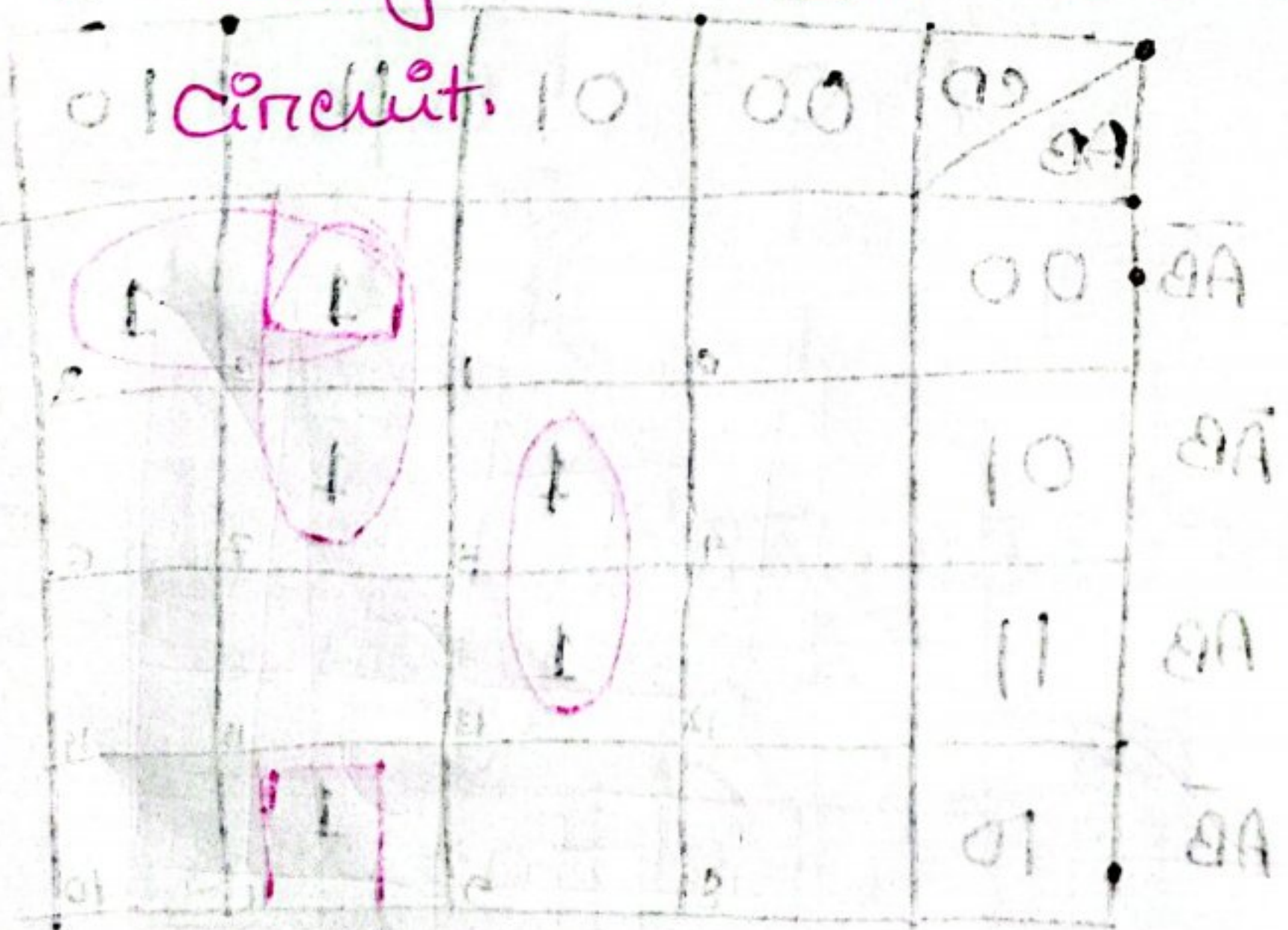
		CD			
		00	01	11	10
AB	$\bar{A}\bar{B}$	0	1	1	2
	$\bar{A}B$	4	5	7	6
AB	$A\bar{B}$	12	13	15	14
	$AB$	8	9	11	10

$$F = B\bar{C}D + \bar{A}\bar{B}C + \bar{A}CD + \bar{B}CD$$

\* Design a combinational logic circuit  
 whose numbers 10 to 15



\* Design a 4-bit 2's complement combinational logic circuit.



F	D	C	B	A
0	0	0	0	0
0	0	0	1	0
1	0	0	1	1
0	0	1	0	0
1	0	1	0	1
0	0	1	1	0
1	0	1	1	1
0	1	0	0	0
1	1	0	0	1
0	1	0	1	0
1	1	0	1	1
0	1	1	0	0
1	1	1	0	1
0	1	1	1	0
1	1	1	1	1

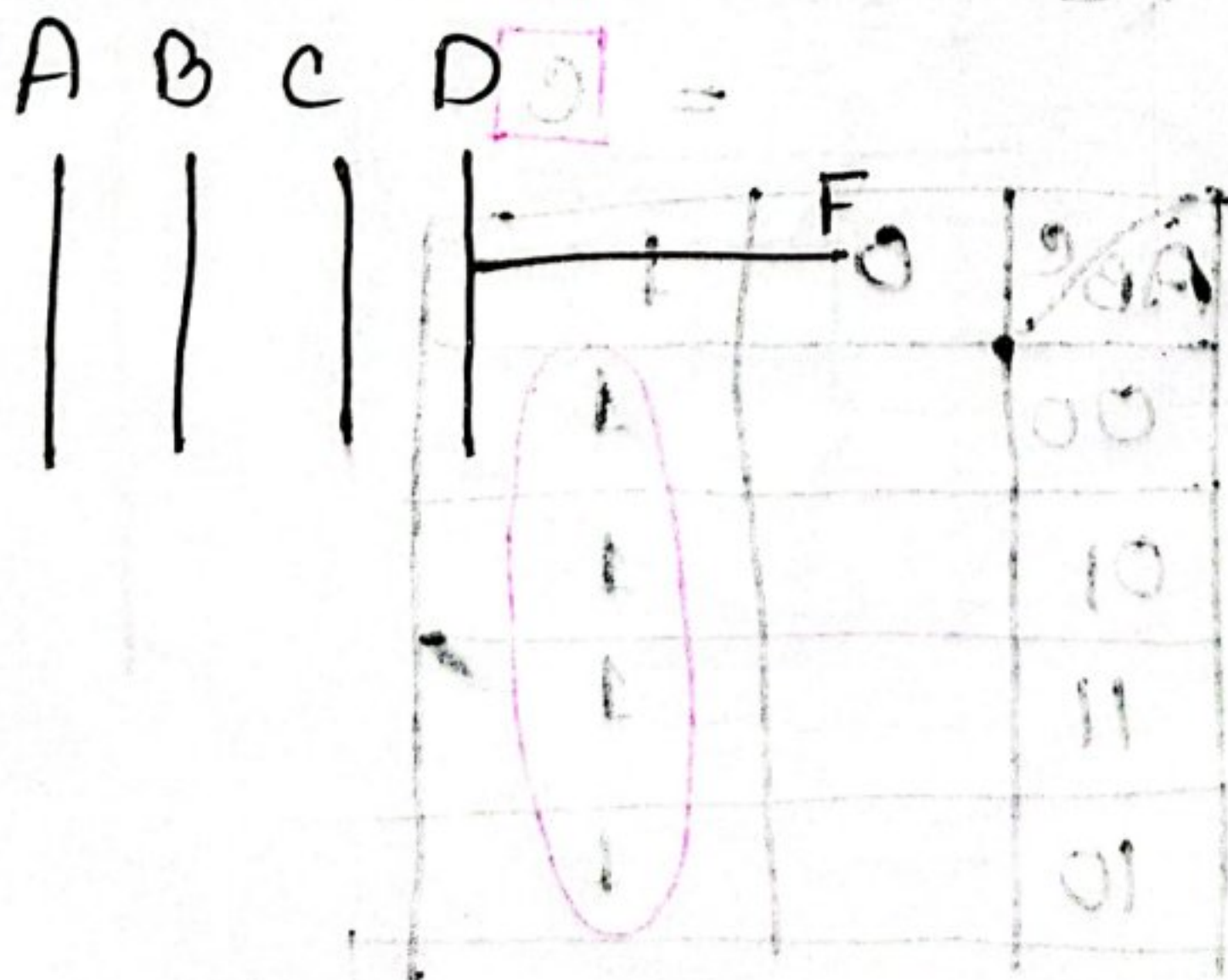
\* Design a 4 bit odd number detector circuit

A	B	C	D	F
0	0	0	0	0
0	0	0	1	1
0	0	1	0	1
0	0	1	1	0
0	1	0	0	1
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	1

$$F = \bar{A}\bar{B}CD + \bar{A}B\bar{C}D + \bar{A}BC\bar{D} + \bar{A}BCD + A\bar{B}\bar{C}D + A\bar{B}C\bar{D} + ABC\bar{D} + ABCD$$

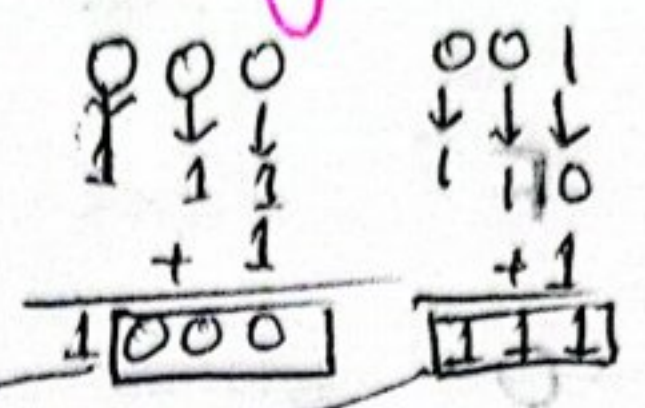
		$\bar{C}\bar{D}$ $\bar{C}D$ $CD$ $C\bar{D}$			
		$\bar{C}\bar{D}$	$\bar{C}D$	$CD$	$C\bar{D}$
AB	00	0	0	0	0
	01	0	1	0	1
10	11	0	0	1	0
	10	0	1	1	0

$$F = D$$



\* Design a 3 bit 2's complement generator circuit

A	B	C	w	x	y
0	0	0	0	0	0
0	0	1	1	1	1
0	1	0	1	1	0
0	1	1	1	0	1
1	0	0	1	0	0
1	0	1	0	1	1
1	1	0	0	1	0
1	1	1	0	0	1



$$W(A,B,C) = \bar{A}\bar{B}C + \bar{A}B\bar{C} + \bar{A}BC + A\bar{B}\bar{C}$$

$$= \bar{A}C + \bar{A}B + A\bar{B}\bar{C}$$

		$\bar{c}$	$c$
$\bar{A}\bar{B}$	00	0	1
$\bar{A}B$	01	1	1
$A\bar{B}$	10	1	0

$$X(A,B,C) = \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}C + ABC$$

$$= B\bar{C} + Bc = B \oplus C$$

$\bar{A}\bar{B}$	00	1
$\bar{A}B$	01	1
$A\bar{B}$	10	1

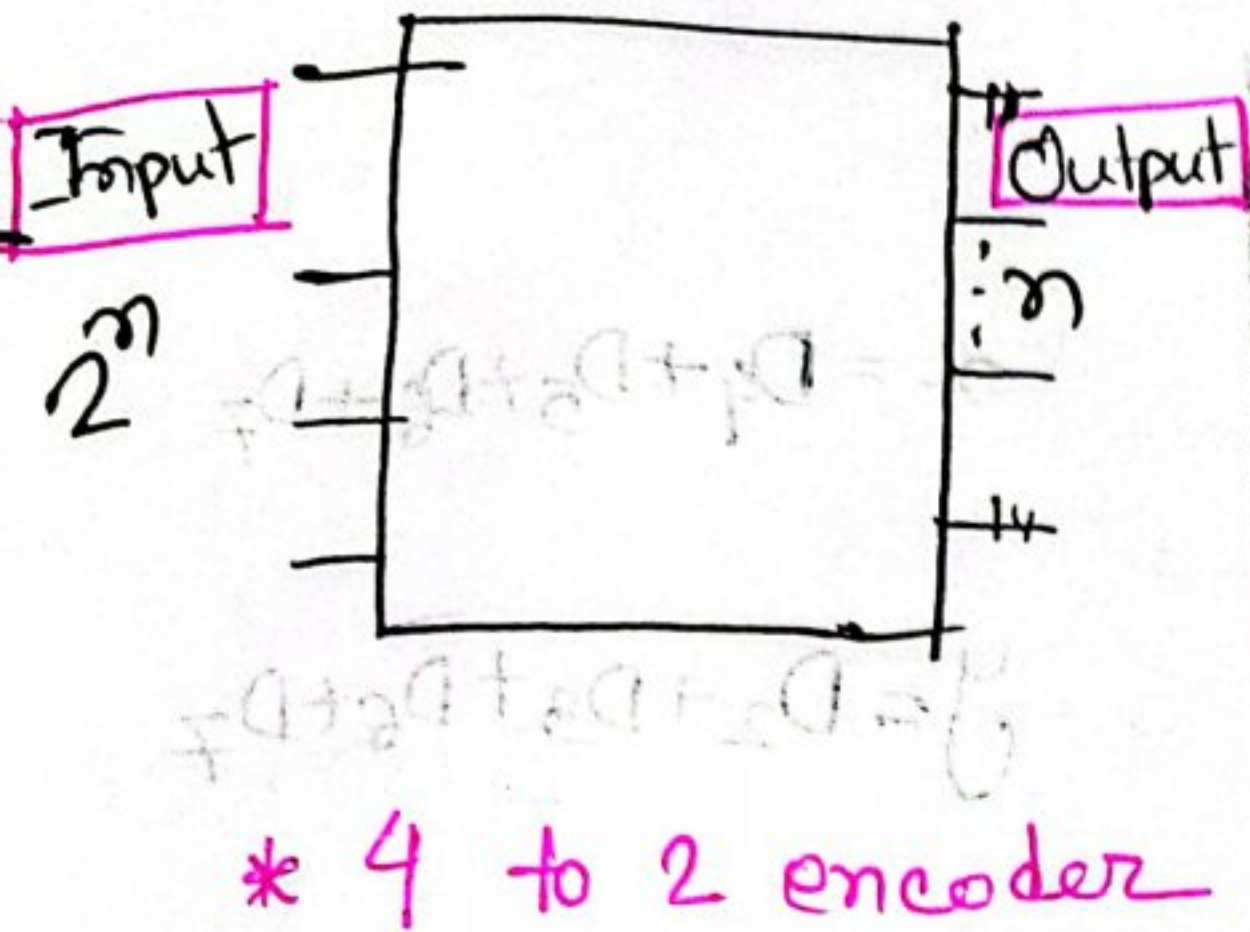
$$Y(A,B,C) = \bar{A}\bar{B}C + \bar{A}BC + A\bar{B}C + ABC$$

$$= C$$

$\bar{A}\bar{B}$	00	1
$\bar{A}B$	01	1
$A\bar{B}$	10	1

# Encoder

An encoder is a digital circuit that has  $2^n$  input lines and  $n$  output lines. It produces binary equivalent of the input.



\* 4 to 2 encoder

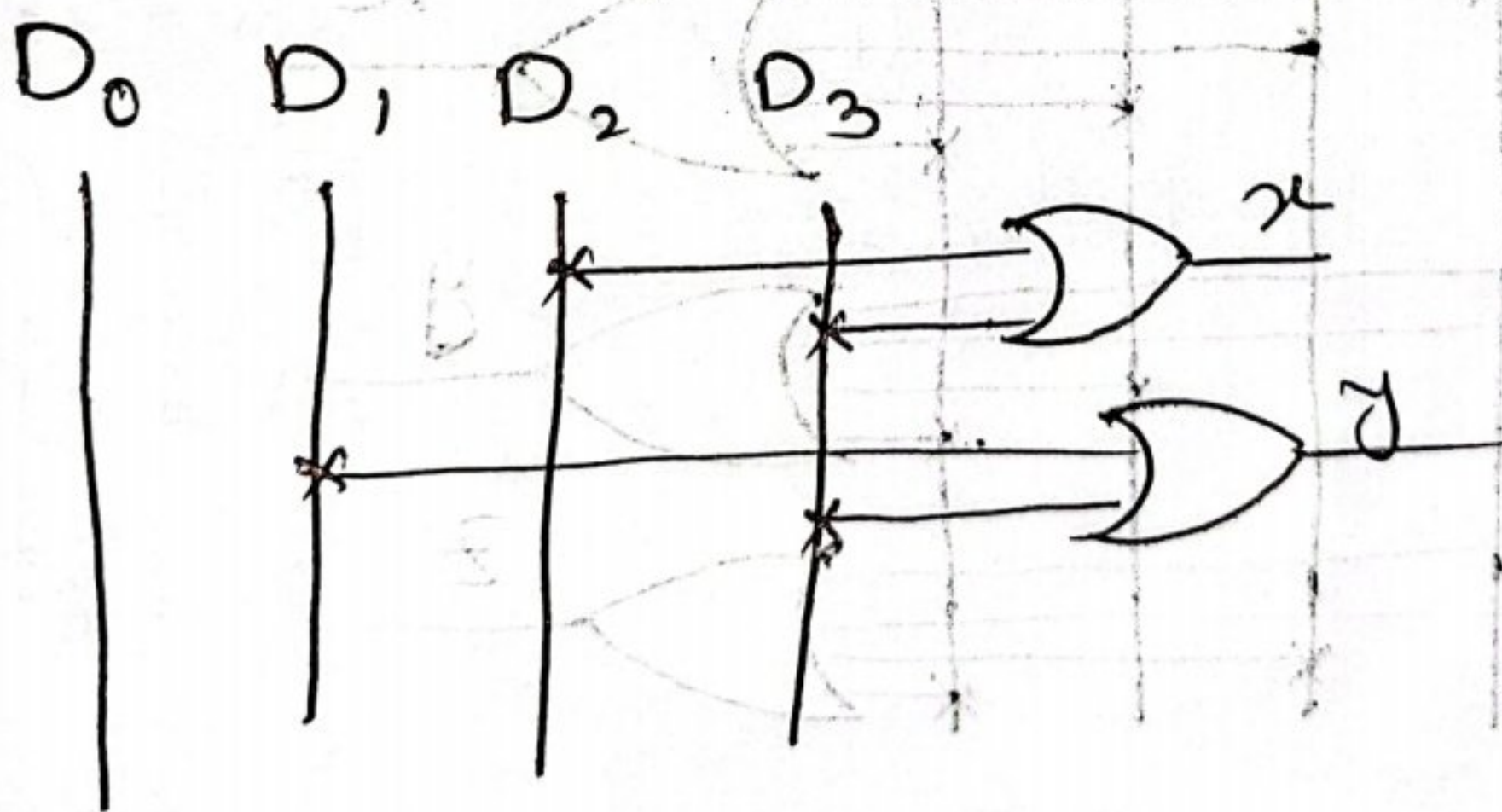
$D_0$	$D_1$	$D_2$	$D_3$	$x$	$y$
1	0	0	0	0	0
0	1	0	0	0	1
0	0	1	0	1	0
0	0	0	1	1	1

$$x = \bar{D}_0 \bar{D}_1 D_2 \bar{D}_3 + \bar{D}_0 \bar{D}_1 \bar{D}_2 D_3$$

Not like this

$$x = D_2 + D_3 \quad \checkmark$$

$$y = D_1 + D_3 \quad \checkmark$$



# \* Design an 8 to 3 encoder

Foragers

$D_0$	$D_1$	$D_2$	$D_3$	$D_4$	$D_5$	$D_6$	$D_7$	$x$	$y$	$z$
1	0	0	0	0	0	0	0	0	0	0
0	1	0	0	0	0	0	0	0	0	0
0	0	1	0	0	0	0	0	0	1	0
0	0	0	1	0	0	0	0	0	1	1
0	0	0	0	1	0	0	0	1	0	0
0	0	0	0	0	1	0	0	1	0	1
0	0	0	0	0	0	1	0	1	1	0
0	0	0	0	0	0	0	1	1	1	1

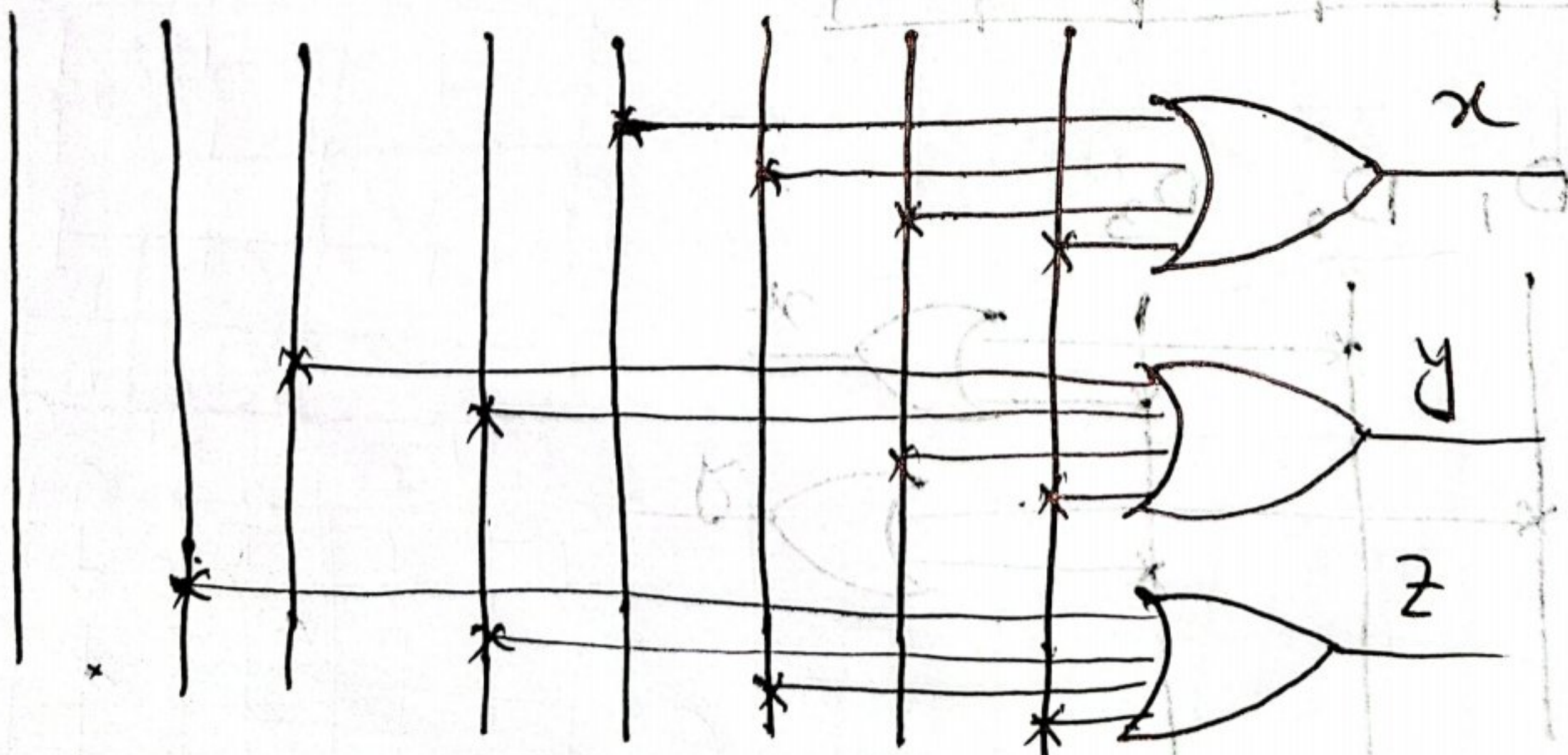
$$x = D_4 + D_5 + D_6 + D_7$$

$$y = D_2 + D_3 + D_6 + D_7$$

Subarna 2 of P \*

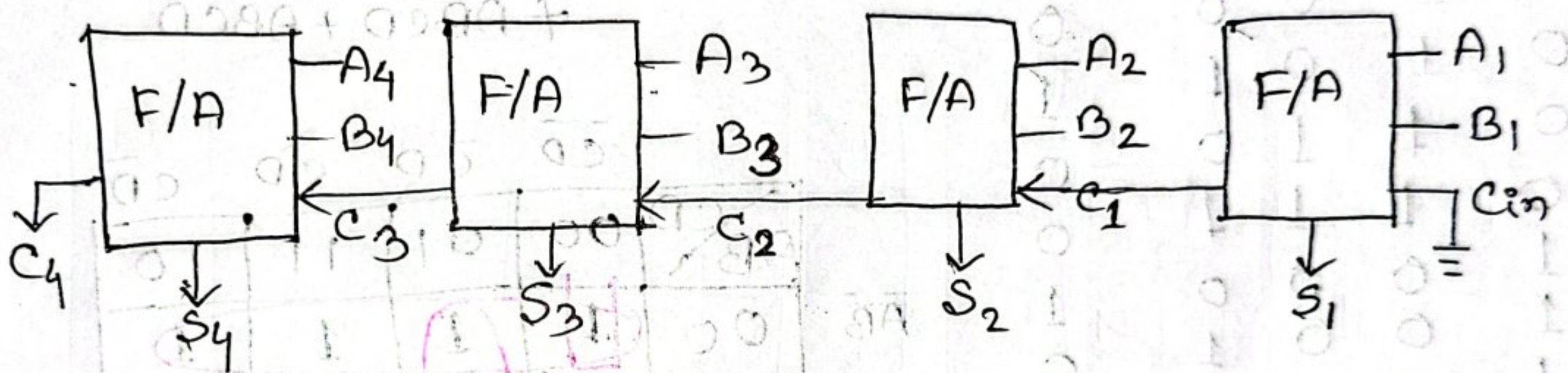
$$z = D_1 + D_3 + D_5 + D_7$$

$D_0$   $D_1$   $D_2$   $D_3$   $D_4$   $D_5$   $D_6$   $D_7$



\* Design a combinational logic circuit to solve the following problem.

$$\begin{array}{r}
 A_4 \quad A_3 \quad A_2 \quad A_1 \\
 B_4 \quad B_3 \quad B_2 \quad B_1 \\
 \hline
 C_4 \quad S_4 \quad S_3 \quad S_2 \quad S_1
 \end{array}$$



$$S_1 = A_1 \oplus B_1 \oplus C_{in}$$

$$C_1 = C_{in} (A_1 \oplus B_1) + A_1 B_1$$

$$S_2 = A_2 \oplus B_2 \oplus C_1$$

$$C_2 = C_1 (A_2 \oplus B_2) + A_2 B_2$$

$$S_3 = A_3 \oplus B_3 \oplus C_2$$

$$C_3 = C_2 (A_3 \oplus B_3) + A_3 B_3$$

$$S_4 = A_4 \oplus B_4 \oplus C_3$$

$$C_4 = C_3 (A_4 \oplus B_4) + A_4 B_4$$

\* Design a fibonacci number detector that can detect fibonacci numbers up to 15.

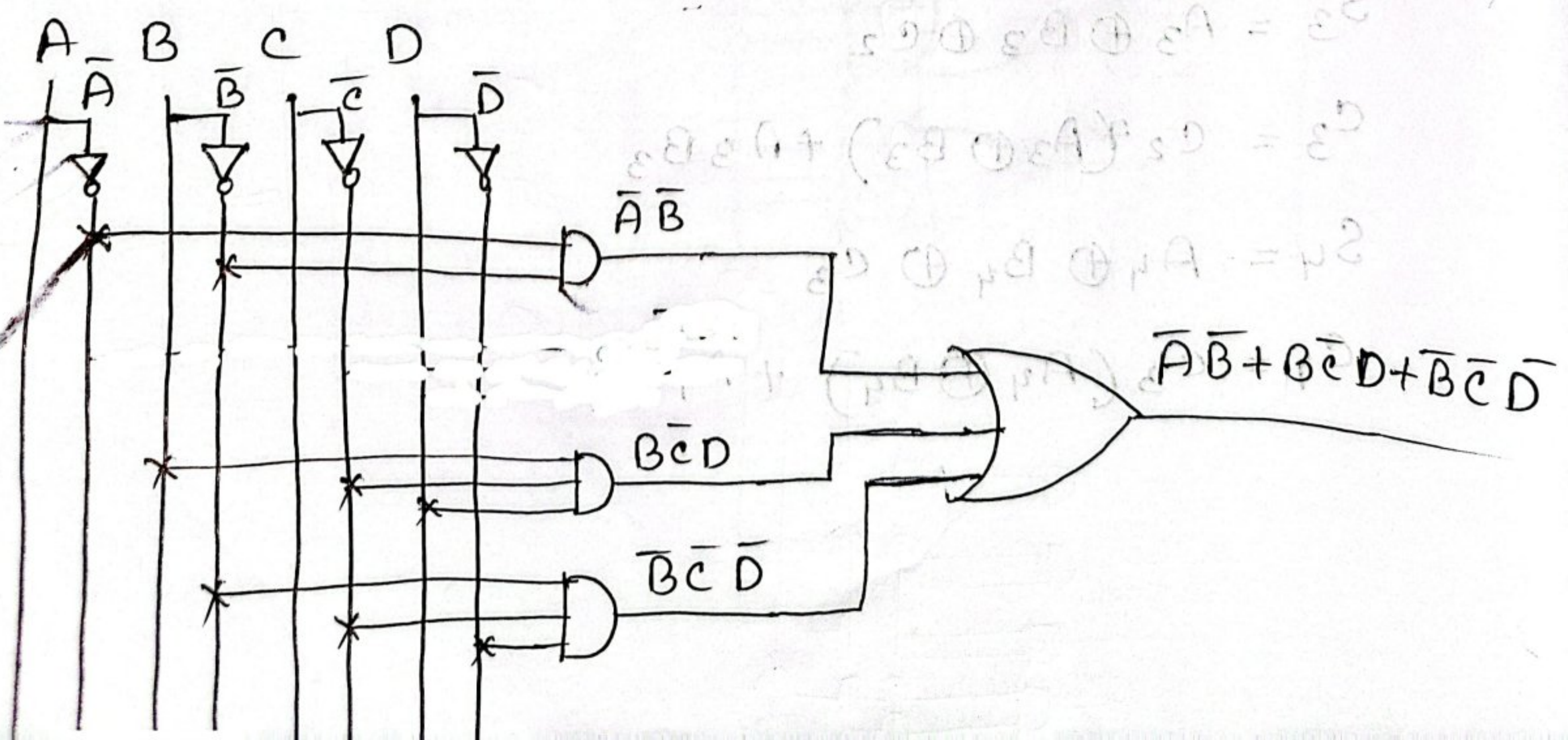
0 1 1 2 3 5 8 13

A	B	C	D	F
0	0	0	0	1
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	0

$$F = \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}B\bar{C}D + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D + \bar{A}B\bar{C}\bar{D}$$

AB \ CD	00	01	11	10
$\bar{A}\bar{B}$	1	1	1	1
$\bar{A}B$		1		
$A\bar{B}$			1	
$AB$				

$$F = \bar{A}\bar{B} + B\bar{C}D + \bar{B}\bar{C}\bar{D}$$



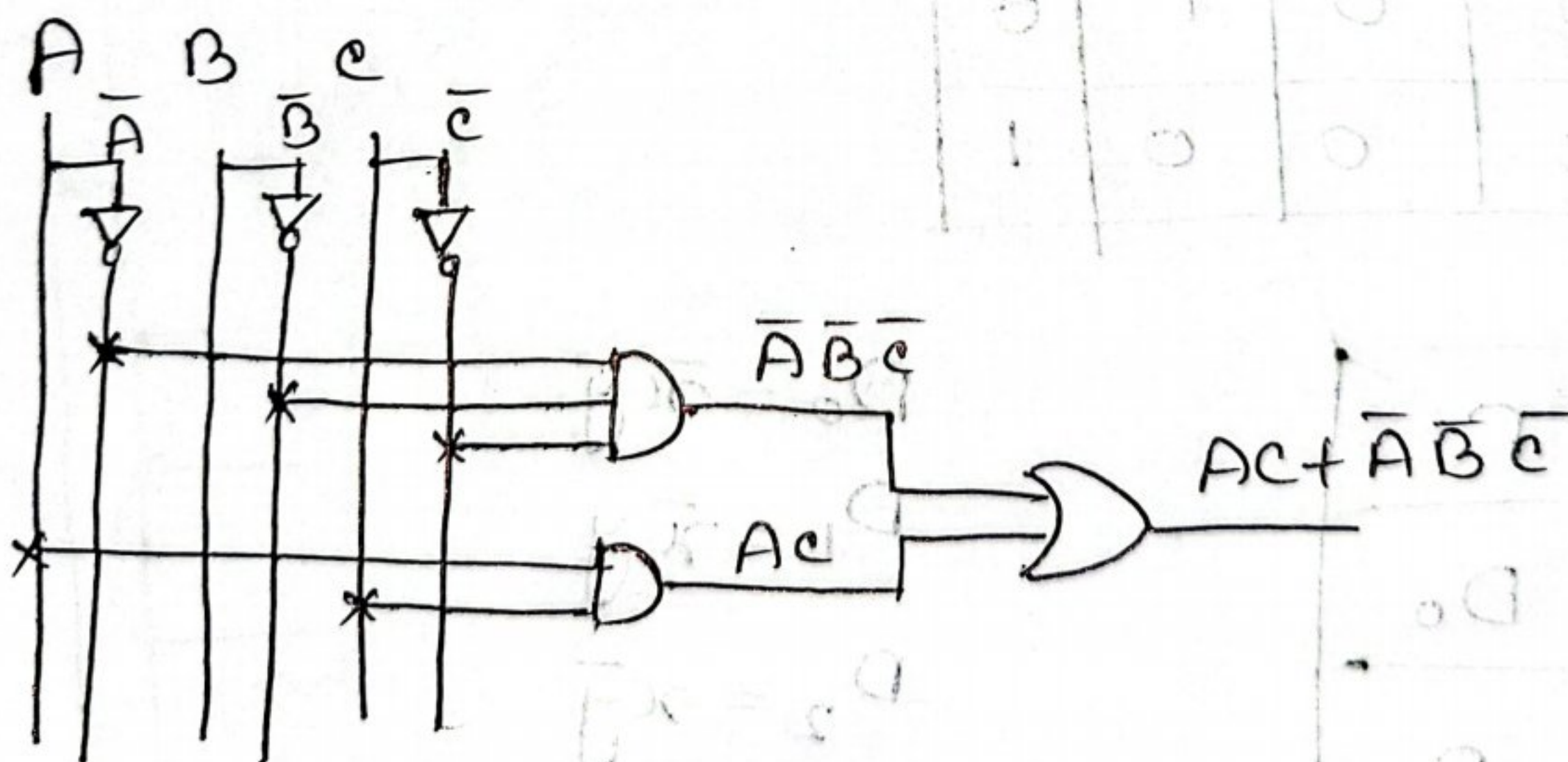
\* Design an elevator circuit for a 7 floored building which will stop at Ground, 5th and top floor only

A	B	C	F
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

$$F = \bar{A}\bar{B}\bar{C} + A\bar{B}C + ABC$$

$$= \bar{A}\bar{B}\bar{C} + AC$$

	$\bar{C}$	C
AB	0	1
$\bar{A}\bar{B}$	0 0	1 0
$\bar{A}B$	0 1	0 1
AB	1 1	0 1
AB	1 0	1 1



0	0	0	0
0	1	0	0
1	0	0	0
1	1	0	0
0	0	1	0
0	1	1	0
1	0	1	1
1	1	1	1

# Decoder

A decoder is a combinational circuit that converts binary information from  $n$  input lines to a maximum of  $2^n$  output lines.

\* Design a 2 to 4 decoder

	B	A
0	0	0
0	0	1
0	1	0
0	1	1
1	0	0
1	0	1
1	1	0
1	1	1

x	y	D <sub>0</sub>	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>
0	0	1	0	0	0
0	1	0	1	0	0
1	0	0	0	1	0
1	1	0	0	0	1

OR →

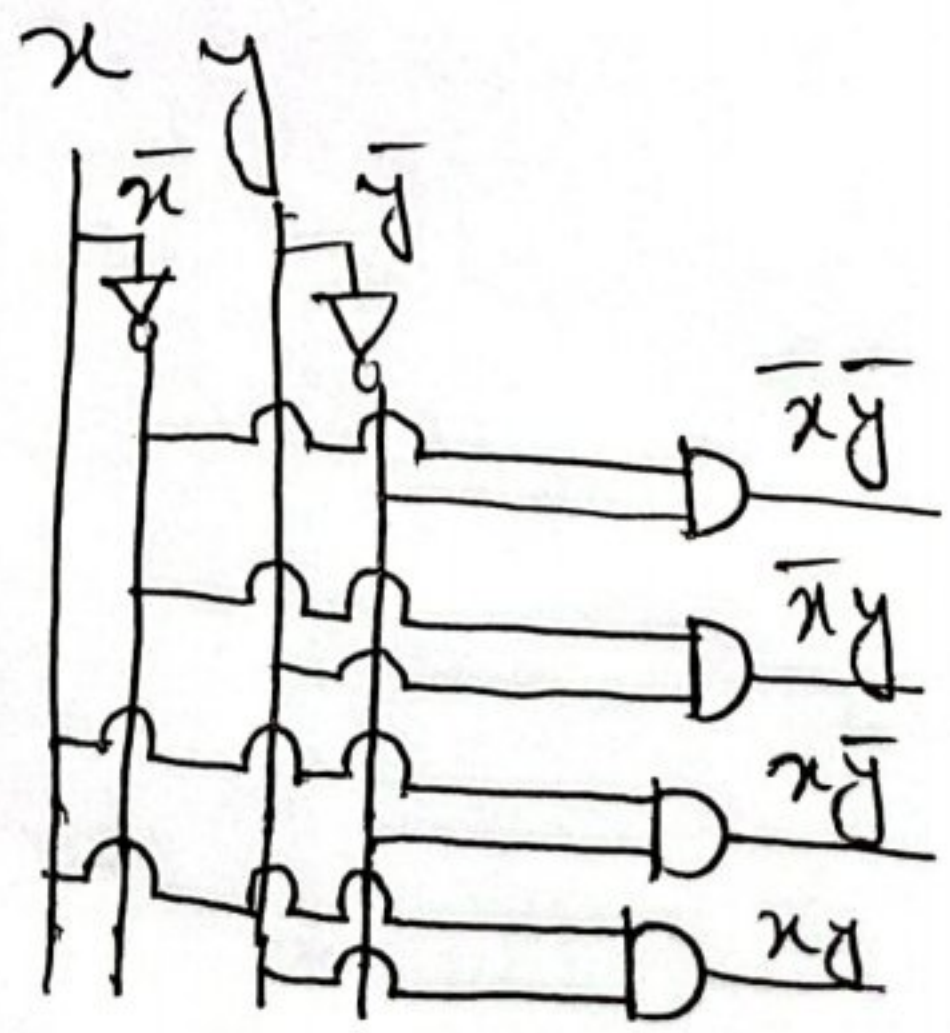
x	y	F
0	0	D <sub>0</sub>
0	1	D <sub>1</sub>
1	0	D <sub>2</sub>
1	1	D <sub>3</sub>

$$D_0 = \bar{x}\bar{y}$$

$$D_1 = \bar{x}y$$

$$D_2 = x\bar{y}$$

$$D_3 = xy$$



# \* Design a 3 to 8 decoder

x	y	z	F
0	0	0	D <sub>0</sub>
0	0	1	D <sub>1</sub>
0	1	0	D <sub>2</sub>
0	1	1	D <sub>3</sub>
1	0	0	D <sub>4</sub>
1	0	1	D <sub>5</sub>
1	1	0	D <sub>6</sub>
1	1	1	D <sub>7</sub>

$$D_0 = \bar{x}\bar{y}\bar{z}$$

$$D_1 = \bar{x}\bar{y}z$$

$$D_2 = \bar{x}y\bar{z}$$

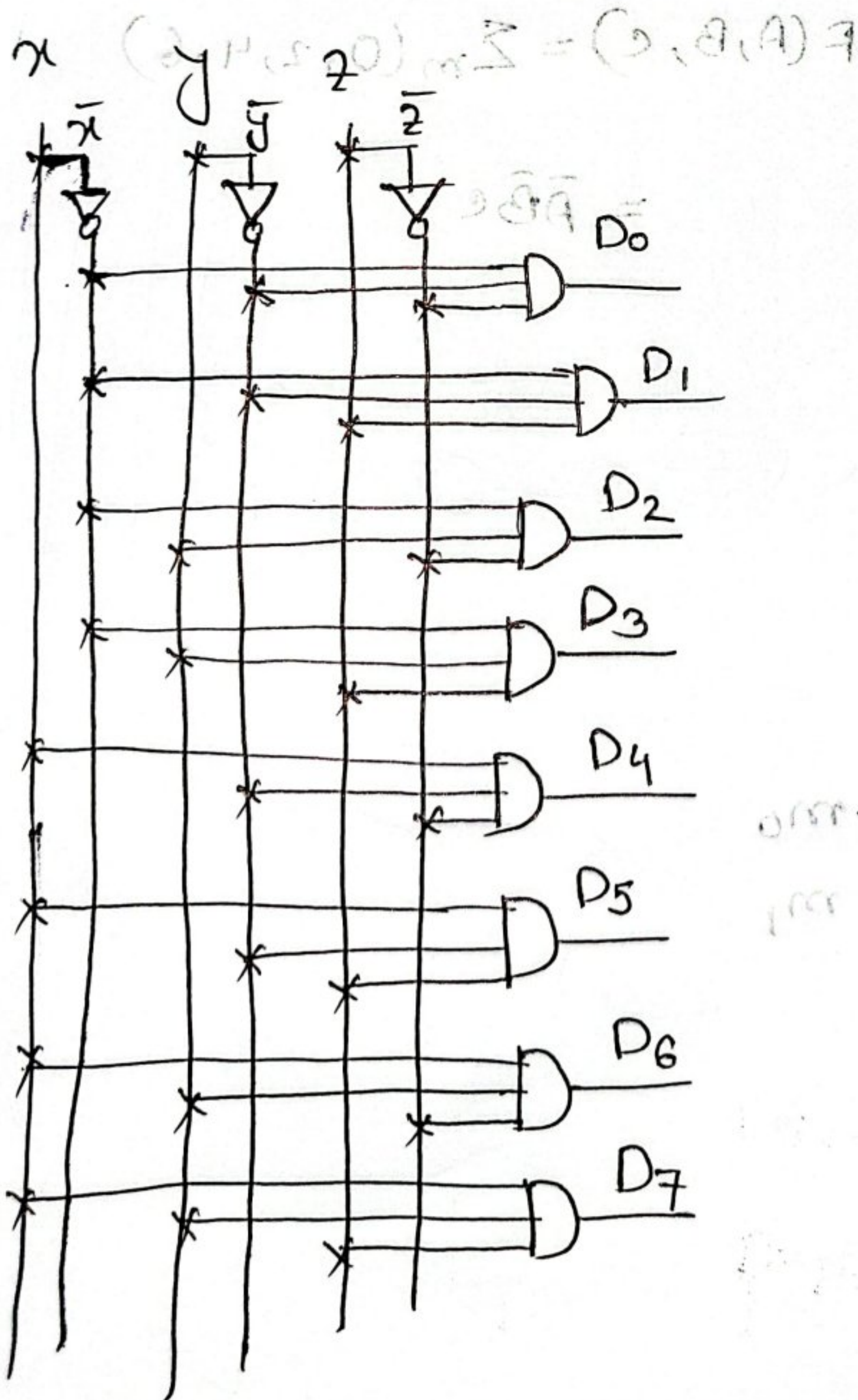
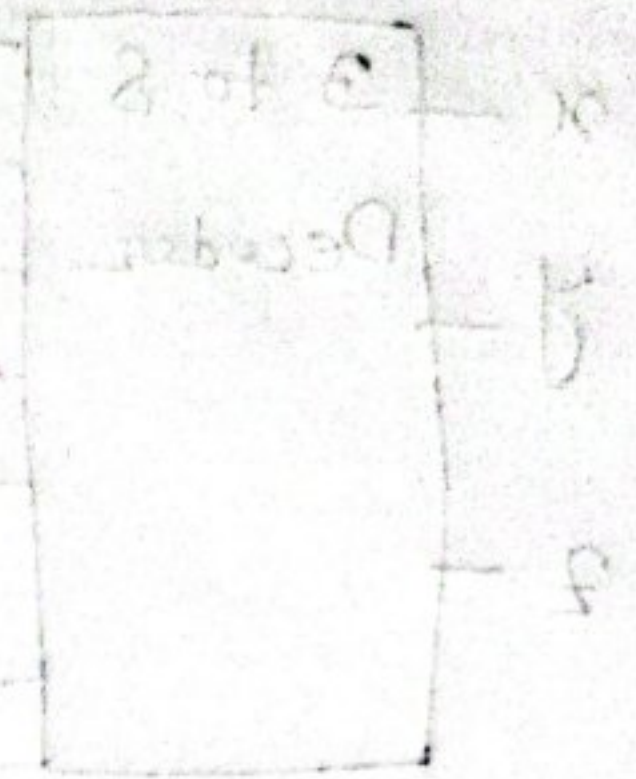
$$D_3 = \bar{x}yz$$

$$D_4 = x\bar{y}\bar{z}$$

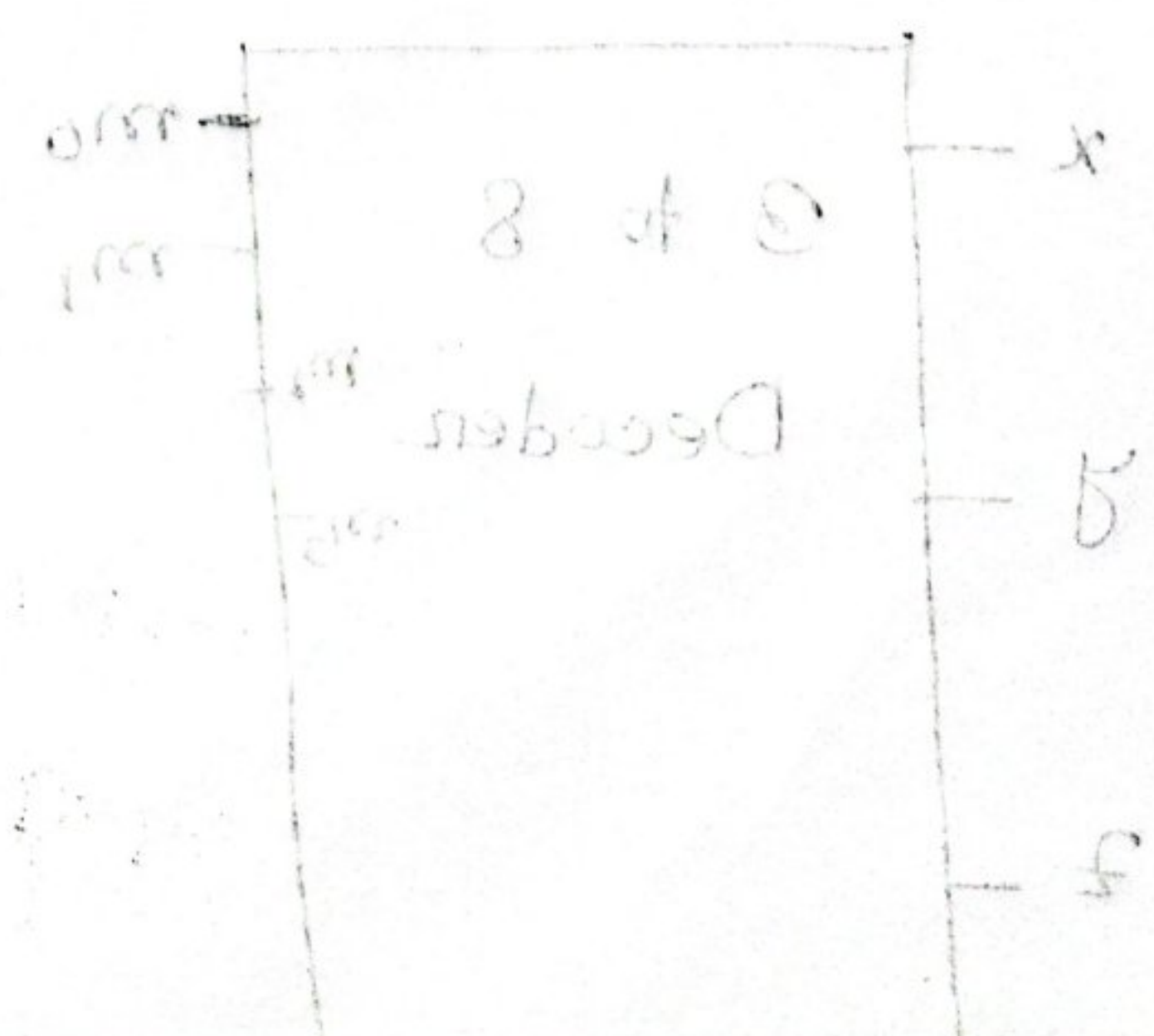
$$D_5 = x\bar{y}z$$

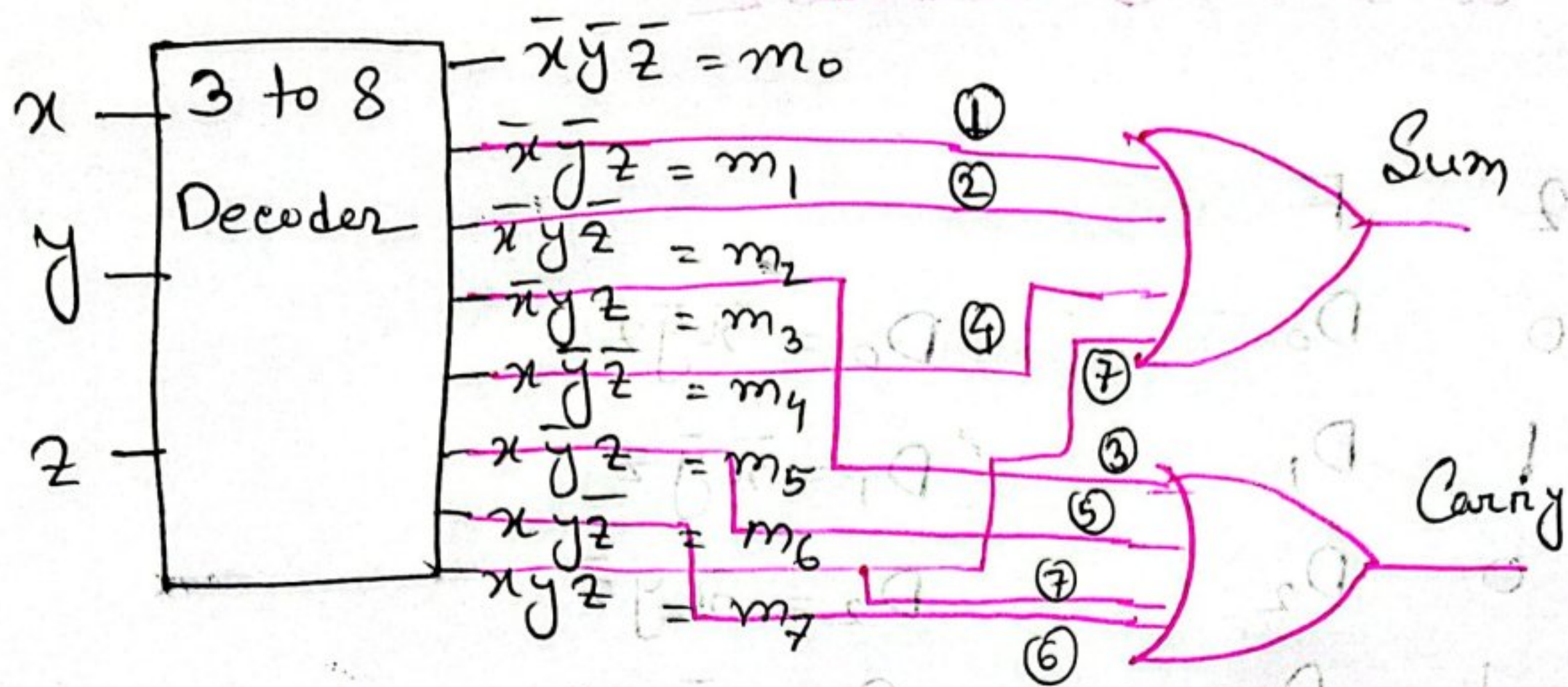
$$D_6 = xy\bar{z}$$

$$D_7 = xyz$$



F	A	B	C
0	0	0	0
1	0	0	1
0	0	1	0
1	0	1	1
0	1	0	0
1	1	0	1
0	1	1	0
1	1	1	1





Sum =  $\sum m(1, 2, 4, 7)$

Carry =  $\sum m(3, 5, 6, 7)$

\* Design a 3 bit even number detector circuit using decoder.

A	B	C	F
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

$F(A, B, C) = \sum m(0, 2, 4, 6)$

